

# CUFSM Advanced Functions

- Boundary conditions
- Constraints
- Springs
- Multiple materials
- Orthotropic Material

# Boundary conditions

- Longitudinal boundary conditions (fixity) can be set in the finite strip model
- Modeling classic problems requires using this feature
  - simply supported plate
  - fixed plate
- Special cases may exist where artificial boundary conditions are added in an analysis to examine a particular buckling mode in exclusion of other modes (see Advanced Ideas for more on this)
- Symmetry and anti-symmetry conditions may be modeled by modifying the boundary conditions

# Boundary conditions continued

- How to
- Simply supported plate example
- Fixed-free plate example
- Flange only model
- Symmetry model on a hat in bending example



### Material Properties

mat# | Ex | Ey | vx | vy | Gxy

100 29500.00 29500.00 0.30 0.30 11346.15

### Nodes

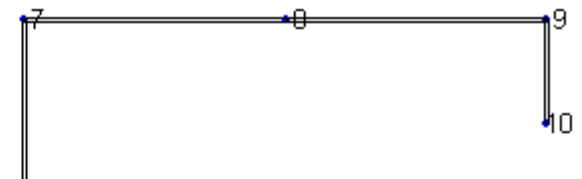
node# | x | z | xdof | zdof | ydof | qdof | stress

1	5.00	1.0	1	1	1	1	33.33
2	5.00	0.0	1	1	1	1	50.00
3	2.50	0.0	1	1	1	1	50.00
4	0.00	0.0	1	1	1	1	50.00
5	0.00	3.0	1	1	1	1	6.67
6	0.00	6.0	1	1	1	1	6.67
7	0.00	9.0	1	1	1	1	0.00
8	2.50	9.0	1	1	1	1	0.00
9	5.00	9.0	1	1	1	1	0.00
10	5.00	8.0	0	1	1	1	33.33

### Elements

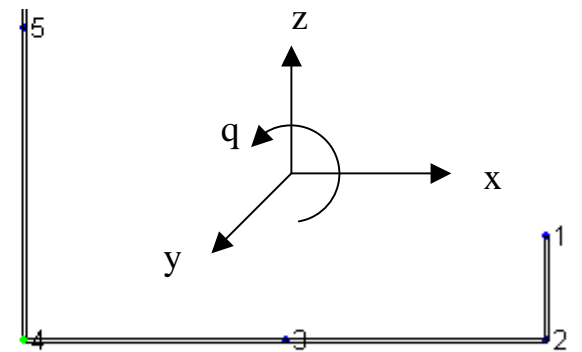
elem# | nodei | nodej | thickness | mat#

1	1	2	0.040000	100
2	2	3	0.040000	100
3	3	4	0.040000	100
4	4	5	0.040000	100
5	5	6	0.040000	100
6	6	7	0.040000	100
7	7	8	0.040000	100
8	8	9	0.040000	100
9	9	10	0.040000	100



These columns of ones set the boundary conditions for the model. A 1 implies that the degree of freedom is free along its longitudinal edge. All models are simply supported at the ends due to the choice of shape function in the finite strip method.

For models of members these always remain 1, however if longitudinal restraint should be modeled then the appropriate degree of freedom (direction) should be changed from a 1 to a 0.



### Lengths

1.0 2.0 3.0 4.0 5.0 6.0 7.0 8.0 9.0 10.0 11.0 12.0 13.0 14.0 15.0 20.0 30.0 40.0 50.0 60.0 70.0 80.0 90.0 100.0 200.0 300.0 400.0 500.0 600.0 700.0 800.0 900.0 1000.0

### Springs

node# | DOF(x=1,z=2,y=3,theta=4) | kspring | kflag

0

### Constraints

node#e | DOFe | coeff. | node#k | DOFk

0



<b>Material Properties</b> ? mat#   E <sub>x</sub>   E <sub>y</sub>   ν <sub>x</sub>   ν <sub>y</sub>   G <sub>xy</sub> 100 29500.00 29500.00 0.30 0.30 11346.00	C/Z template Double Elem. help
<b>Nodes</b> ? node#   x   z   x dof   z dof   y dof   q dof   stress 1 0.00 0.00 0 0 1 1 1.00 2 2.50 0.00 1 1 1 1 1.00 3 5.00 0.00 1 1 1 1 1.00 4 7.50 0.00 1 1 1 1 1.00 5 10.00 0.00 1 0 1 1 1.00	Update Plot Plot Options: <input checked="" type="checkbox"/> node # <input type="checkbox"/> element # <input type="checkbox"/> material # <input type="checkbox"/> stress mag. <input type="checkbox"/> stress dist. <input type="checkbox"/> coordinate: <input checked="" type="checkbox"/> constraints <input checked="" type="checkbox"/> springs <input checked="" type="checkbox"/> origin
<b>Elements</b> ? elem#   nodei   nodej   thickness   mat# 1 1 2 0.100000 100 2 2 3 0.100000 100 3 3 4 0.100000 100 4 4 5 0.100000 100	

### Simply supported plate in pure compression

Plate is 10 in. wide and  $t = 0.10$  in., material is steel.

The x and z degree of freedom at node 1 have been supported by changing the appropriate 1's to 0's.

The z degree of freedom at node 5 has been supported by changing the appropriate 1 to 0.

Green boxes appear at 1 and 5 to indicate some boundary conditions have been changed at this node.



<b>Lengths</b> ? 4.0 6.0 8.0 10.0 12.0 14.0 16.0 18.0 20.0	
<b>Springs</b> ? node#   DOF(x=1,z=2,y=3,theta=4)   kspring   kflag 0	<b>Constraints</b> ? node#e   DOFe   coeff.   node#k   DOFk 0

half-wavelength = 10 load factor = 10.6663 mode = 1

$$\text{Theory} \rightarrow f_{cr} = k \frac{\pi^2 E}{12(1-\nu^2)} \left(\frac{t}{b}\right)^2 = 4 \frac{\pi^2 29500}{12(1-0.3^2)} \left(\frac{0.1}{10.0}\right)^2 = 10.66 \text{ksi}$$

Plot Mode ?

2D  3D  Undef.

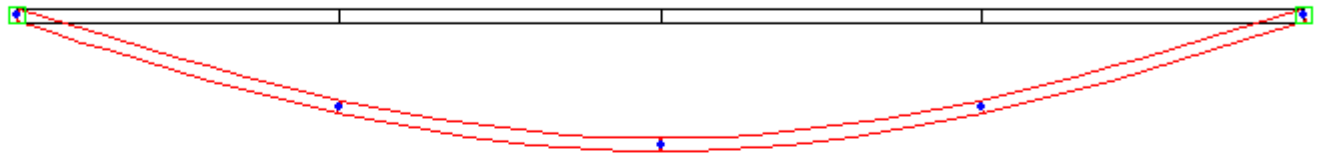
half-wavelength

<-- 10 --> ?

Scale .5

mode <-- 1 --> ?

Stress Distribution ?



Input reference stress is 1.0 ksi. So in this case the load factor is equal to the buckling stress in ksi, i.e., 10.67 ksi. versus 10.66 ksi by hand.

Plot Curve ?

Min.  Log X

xmin 0

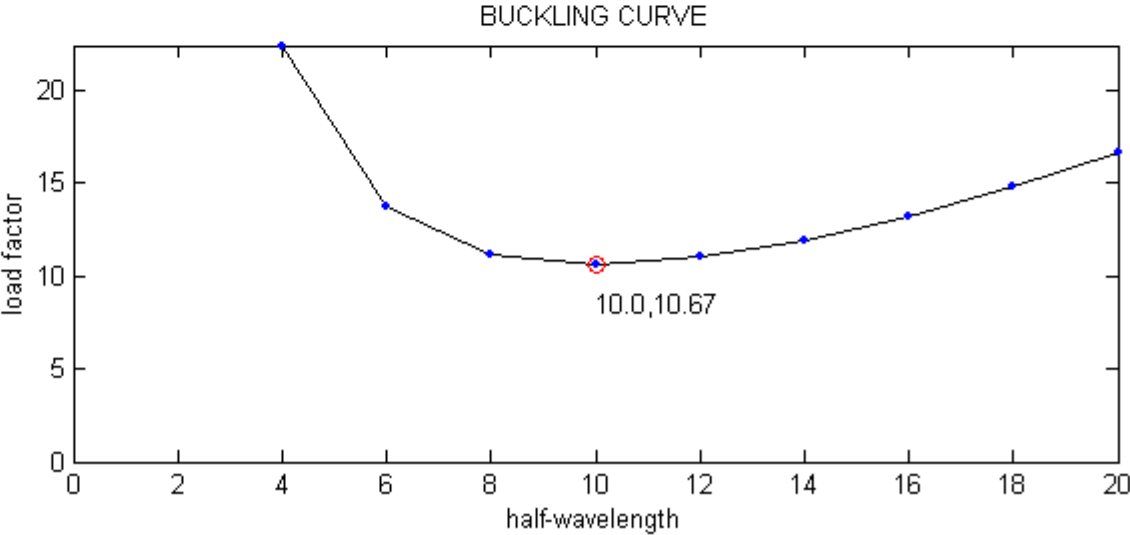
xmax 20

ymin 0

ymax 22.4233

modes <-- 1 --> ?

Text Output ?



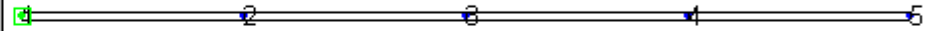
<b>Material Properties</b> ? <small>mat#   Ex   Ey   vx   vy   Gxy</small> 100 29500.00 29500.00 0.30 0.30 11346.00	C/Z template Double Elem. help
<b>Nodes</b> ? <small>node#   x   z   xdof   zdof   ydof   qdof   stress</small> 1 0.00 0.00 0 0 1 0 1.00 2 2.50 0.00 1 1 1 1 1.00 3 5.00 0.00 1 1 1 1 1.00 4 7.50 0.00 1 1 1 1 1.00 5 10.00 0.00 1 1 1 1 1.00	Update Plot Plot Options: <input checked="" type="checkbox"/> node # <input type="checkbox"/> element # <input type="checkbox"/> material # <input type="checkbox"/> stress mag. <input type="checkbox"/> stress dist. <input type="checkbox"/> coordinate: <input checked="" type="checkbox"/> constraints <input checked="" type="checkbox"/> springs <input checked="" type="checkbox"/> origin
<b>Elements</b> ? <small>elem#   nodei   nodej   thickness   mat#</small> 1 1 2 0.100000 100 2 2 3 0.100000 100 3 3 4 0.100000 100 4 4 5 0.100000 100	

**Fixed-free plate in pure compression**

Plate is 10 in. wide and  $t = 0.10$  in., material is steel.

The  $x$ ,  $z$  and  $q$  ( $\theta$ ) degree of freedom at node 1 have been supported by changing the appropriate 1's to 0's.

Green boxes appear at 1 to indicate some boundary conditions have been changed at this node.



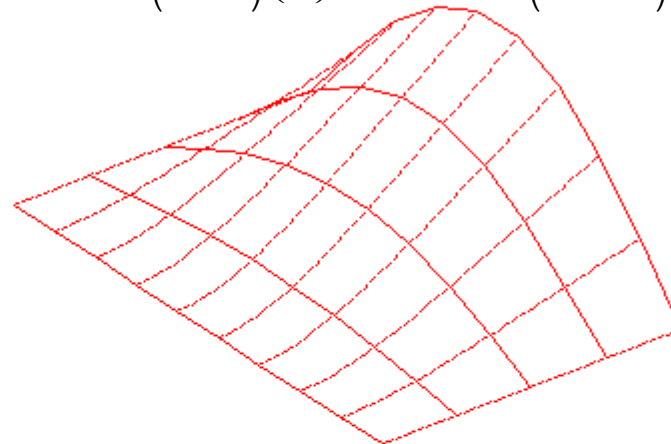
<b>Lengths</b> ? 4.0 6.0 8.0 10.0 12.0 14.0 16.0 18.0 20.0 22.0 24.0 26.0 28.0 30.0
--

<b>Springs</b> ? <small>node#   DOF(x=1,z=2,y=3,theta=4)   kspring   kflag</small> 0
--

<b>Constraints</b> ? <small>node#e   DOFe   coeff.   node#k   DOFk</small> 0
--

half-wavelength = 16 load factor = 3.4167 mode = 1

$$\text{Theory} \rightarrow f_{cr} = k \frac{\pi^2 E}{12(1-\nu^2)} \left(\frac{t}{b}\right)^2 = 1.277 \frac{\pi^2 29500}{12(1-0.3^2)} \left(\frac{0.1}{10.0}\right)^2 = 3.40 \text{ksi}$$



Plot Mode ?

2D  3D  Undef.

half-wavelength

<-- 16 --> ?

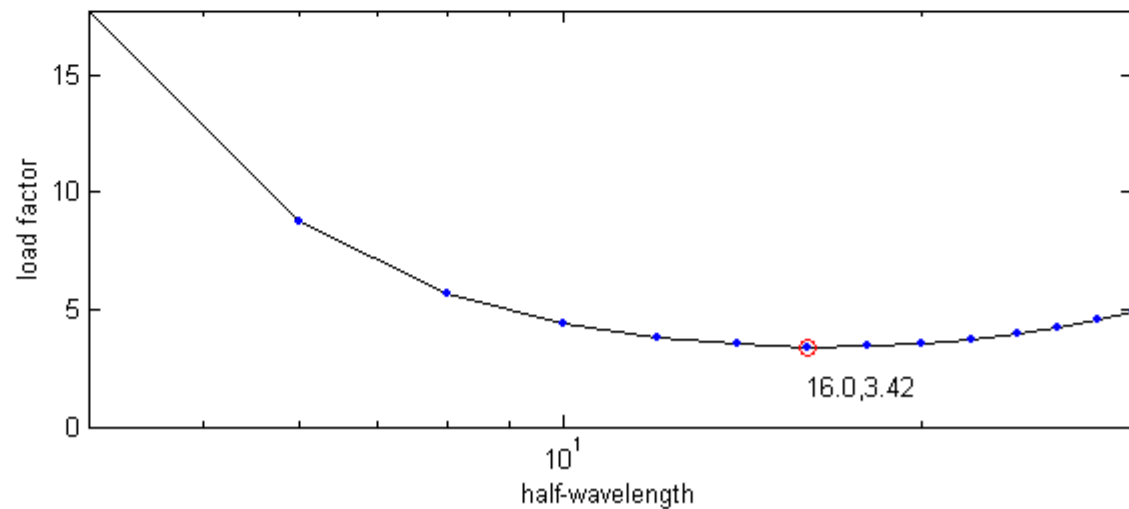
Scale .5

mode <-- 1 --> ?

Stress Distribution ?

Input reference stress is 1.0 ksi. So in this case the load factor is equal to the buckling stress in ksi, i.e., 3.42 ksi. versus 3.40 ksi by hand.

BUCKLING CURVE



Plot Curve ?

Min.  Log X

xmin 0

xmax 30

ymin 0

ymax 17.7774

modes <-- 1 --> ?

Text Output ?



### Material Properties

mat# | E<sub>x</sub> | E<sub>y</sub> | ν<sub>x</sub> | ν<sub>y</sub> | G<sub>xy</sub>

100 29500.00 29500.00 0.30 0.30 11346.15

### Nodes

node# | x | z | xdof | zdof | ydof | qdof | stress

```

1 0.00 0.00 0 0 1 0 1.00
2 2.50 0.00 1 1 1 1 1.00
3 5.00 0.00 1 1 1 1 1.00
4 7.50 0.00 1 1 1 1 1.00
5 10.00 0.00 1 1 1 1 1.00
6 10.00 -1.00 1 1 1 1 1.66
7 10.00 -2.00 1 1 1 1 1.33
            
```

### Elements

elem# | nodei | nodej | thickness | mat#

```

1 1 2 0.100000 100
2 2 3 0.100000 100
3 3 4 0.100000 100
4 4 5 0.100000 100
5 5 6 0.100000 100
6 6 7 0.100000 100
            
```

### Isolated flange in pure compression

Plate is 10 in. wide and  $t = 0.10$  in., material is steel.  
Lip is 2 in. long and the same material and thickness

The x, z and q ( $\theta$ ) degree of freedom at node 1 have been supported by changing the appropriate 1's to 0's. So, the left end is "built-in" or "fixed".

### Lengths

4.0 6.0 8.0 10.0 12.0 14.0 16.0 18.0 20.0 30.0 33.0 37.0 40.0 50.0 60.0 70.0 80.0 90.0 100.0 120.0 160.0 200.0

### Springs

node# | DOF(x=1,z=2,y=3,theta=4) | kspring | kflag

0

### Constraints

node#e | DOFe | coeff. | node#k | DOFk

0

Plot Mode ?

2D  3D  Undef.

half-wavelength

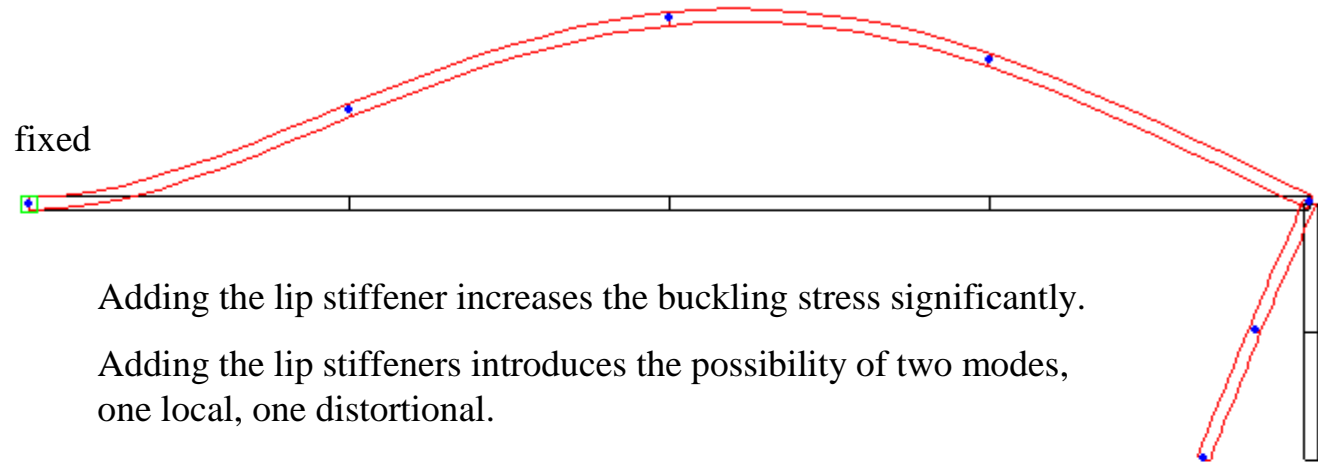
<-- 8 --> ?

Scale .6

mode <-- 1 --> ?

Stress Distribution ?

half-wavelength = 8 load factor = 15.048 mode = 1



Adding the lip stiffener increases the buckling stress significantly.  
 Adding the lip stiffeners introduces the possibility of two modes, one local, one distortional.

Plot Curve ?

Min.  Log X

xmin 0

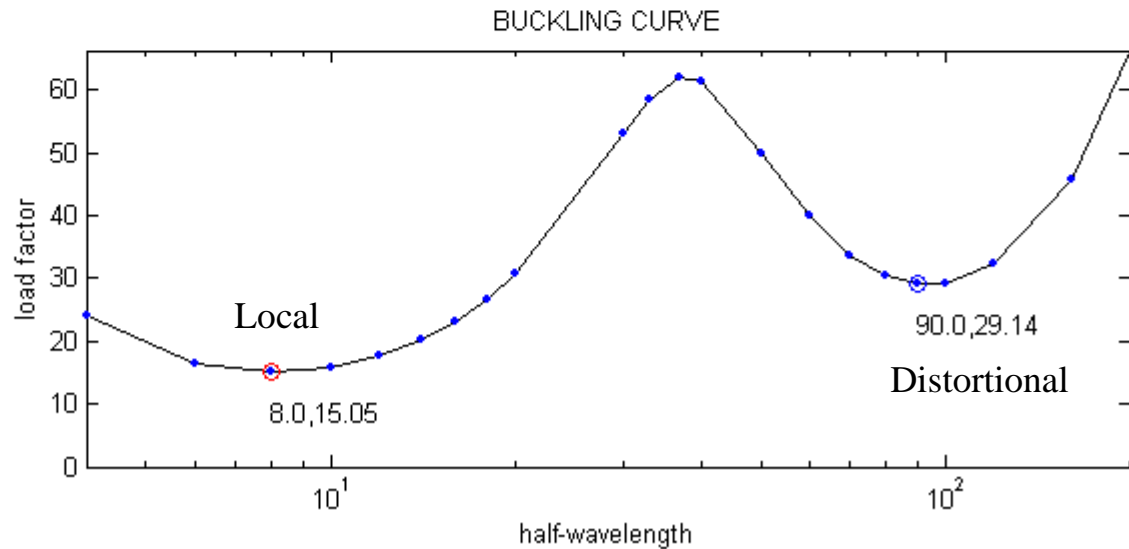
xmax 200

ymin 0

ymax 66.2898

modes <-- 1 --> ?

Text Output ?



### Material Properties

mat# | Ex | Ey | vx | vy | Gxy

100	29500.00	29500.00	0.30	0.30	11346.15
-----	----------	----------	------	------	----------

### Nodes

node# | x | z | xdof | zdof | ydof | qdof | stress

1	-2.00	0.00	1	1	1	-1.75
2	-1.50	0.00	1	1	1	-1.75
3	-1.00	0.00	1	1	1	-1.75
4	-0.50	0.00	1	1	1	-1.75
5	0.00	0.00	1	1	1	-1.75
6	0.00	1.00	1	1	1	-1.06
7	0.00	2.00	1	1	1	-0.37
8	0.00	3.00	1	1	1	0.31
9	0.00	4.00	1	1	1	1.00
10	2.50	4.00	1	1	1	1.00
11	5.00	4.00	1	1	1	1.00

### Elements

elem# | nodei | nodej | thickness | mat#

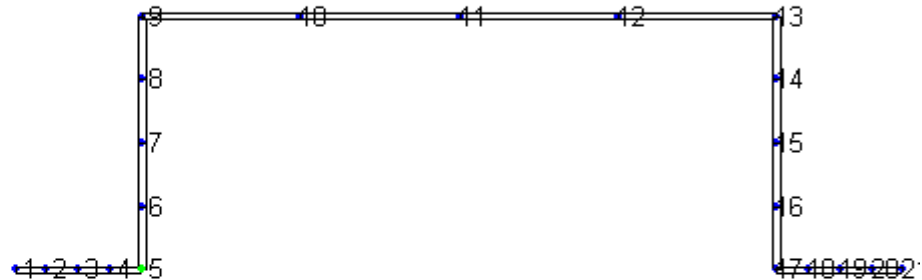
1	1	2	0.100000	100
2	2	3	0.100000	100
3	3	4	0.100000	100
4	4	5	0.100000	100
5	5	6	0.100000	100
6	6	7	0.100000	100
7	7	8	0.100000	100
8	8	9	0.100000	100
9	9	10	0.100000	100
10	10	11	0.100000	100

## Hat in bending - full model

The hat is 2 x 4 x 10 in.

Pure bending is applied as the reference load.

The reference compressive stress for the top flange is 1.0 ksi which results in -1.75 tension for the bottom flange



### Lengths

4.0 6.0 8.0 10.0 12.0 14.0 16.0 18.0 20.0 30.0 33.0 37.0 40.0 50.0 60.0 70.0 80.0 90.0 100.0 120.0 160.0 200.0 300.0 400.0 500.0 600.0 700.0 800.0 900.0 1000.0

### Springs

node# | DOF(x=1,z=2,y=3,theta=4) | kspring | kflag

0
---

### Constraints

node#e | DOFe | coeff. | node#k | DOFk

0
---

### Material Properties

mat# | Ex | Ey | vx | vy | Gxy

100 29500.00 29500.00 0.30 0.30 11346.15

C/Z template  
Double Elem.  
help

### Nodes

node# | x | z | xdof | zdof | ydof | qdof | stress

1	-2.00	0.00	1	1	1	-1.75
2	-1.50	0.00	1	1	1	-1.75
3	-1.00	0.00	1	1	1	-1.75
4	-0.50	0.00	1	1	1	-1.75
5	0.00	0.00	1	1	1	-1.75
6	0.00	1.00	1	1	1	-1.06
7	0.00	2.00	1	1	1	-0.37
8	0.00	3.00	1	1	1	0.31
9	0.00	4.00	1	1	1	1.00
10	2.50	4.00	1	1	1	1.00
11	5.00	4.00	0	1	1	0.100

Update Plot

Plot Options:

node #

element #

material #

stress mag.

stress dist.

coordinate:

constraints

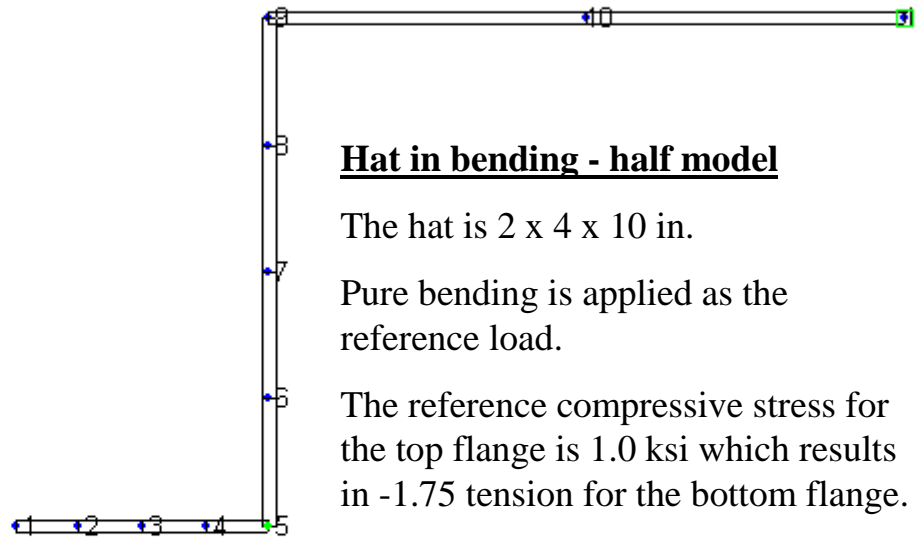
springs

origin

### Elements

elem# | nodei | nodej | thickness | mat#

1	1	2	0.100000	100
2	2	3	0.100000	100
3	3	4	0.100000	100
4	4	5	0.100000	100
5	5	6	0.100000	100
6	6	7	0.100000	100
7	7	8	0.100000	100
8	8	9	0.100000	100
9	9	10	0.100000	100
10	10	11	0.100000	100



### Hat in bending - half model

The hat is 2 x 4 x 10 in.

Pure bending is applied as the reference load.

The reference compressive stress for the top flange is 1.0 ksi which results in -1.75 tension for the bottom flange.

Symmetry conditions are enforced at mid-width of the top flange, note the degrees of freedom changed to 0 at node 11 in the Nodes list to the left.

### Lengths

4.0 6.0 8.0 10.0 12.0 14.0 16.0 18.0 20.0 30.0 33.0 37.0 40.0 50.0 60.0 70.0 80.0 90.0 100.0 120.0 160.0 200.0 300.0 400.0 500.0 600.0 700.0 800.0 900.0 1000.0

### Springs

node# | DOF(x=1,z=2,y=3,theta=4) | kspring | kflag

0

### Constraints

node#e | DOFe | coeff. | node#k | DOFk

0

Plot Mode ?

2D  3D  Undef.

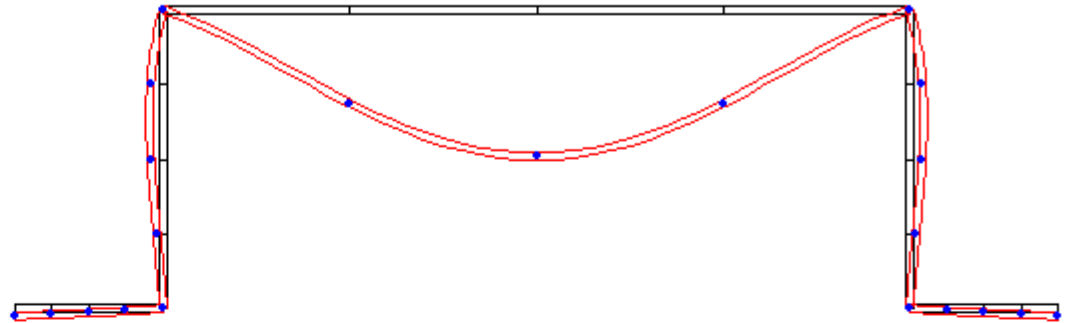
half-wavelength

<-- 8 --> ?

Scale .7 S

mode <-- 1 --> ?

file <-- 2 --> ?



full model local buckling stress in compression = 15.11 ksi

half-wavelength = 8 load factor = 15.1092 mode = 1

filename = hat\_full\_model.mat

filename = 2

Plot Curve ?

Min.  Log X

xmin 0

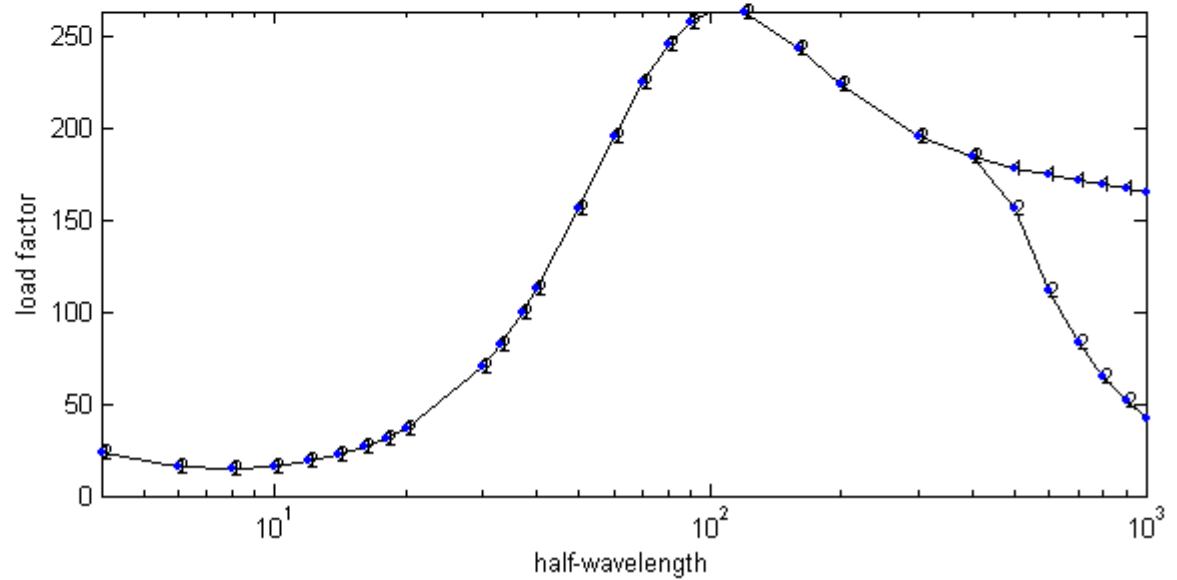
xmax 1000

ymin 0

ymax 264.1734

modes <-- 1 --> ?

plot files = 1 2 ?



Plot Mode ?

2D  3D  Undef.

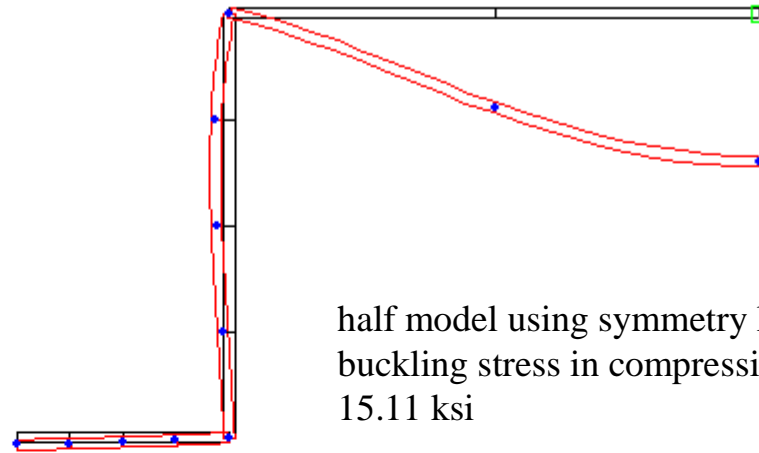
half-wavelength

<-- 8 --> ?

Scale -1 S

mode <-- 1 --> ?

file <-- 1 --> ?



half-wavelength = 8      load factor = 15.1092      mode = 1  
 filename = hat\_halfsymm\_model.mat  
 filenumber = 1

Plot Curve ?

Min.  Log X

xmin 0

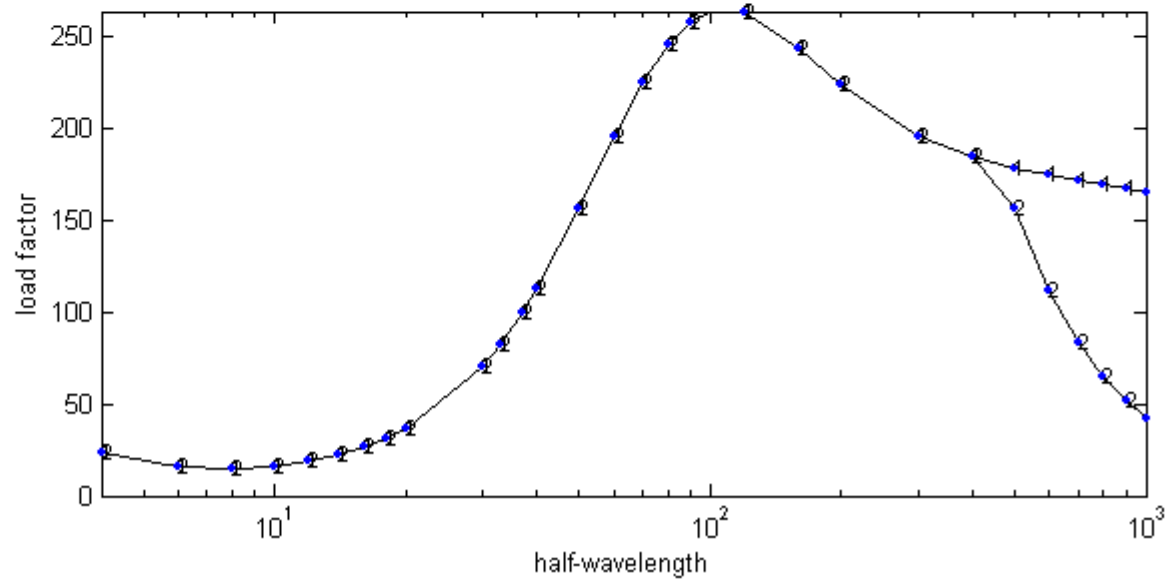
xmax 1000

ymin 0

ymax 264.1734

modes <-- 1 --> ?

plot files = 1 2 ?



# Constraints

- You may write an equation constraint: this enforces the deflection (rotation) of one node to be a function of the deflection (rotation) of a second node.
- Modeling external attachments may be aided by using this feature
  - an external bar that forces two nodes to have the same translation but leaves them otherwise free
  - a brace connecting two members (you can model multiple members in CUFSM)
- Special cases may exist where artificial equation constraints are added in an analysis to examine a particular buckling mode in exclusion of other modes (see Advanced Ideas for more on this)

# Constraints continued

- How to
- Connected lips in a member
- Multiple connected members



**Material Properties** ?

mat# | Ex | Ey | vx | vy | Gxy

100 29500.00 29500.00 0.30 0.30 11346.15

C/Z template  
Double Elem.  
help

**Nodes** ?

node# | x | z | xdof | zdof | ydof | qdof | stress

1	5.00	1.00	1	1	1	1.00
2	5.00	0.00	1	1	1	1.00
3	2.50	0.00	1	1	1	1.00
4	0.00	0.00	1	1	1	1.00
5	0.00	3.00	1	1	1	1.00
6	0.00	6.00	1	1	1	1.00
7	0.00	9.00	1	1	1	1.00
8	2.50	9.00	1	1	1	1.00
9	5.00	9.00	1	1	1	1.00
10	5.00	8.00	1	1	1	1.00

Update Plot

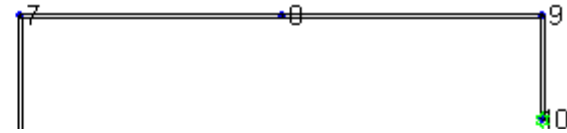
Plot Options:

- node #
- element #
- material #
- stress mag.
- stress dist.
- coordinate:
- constraints
- springs
- origin

**Elements** ?

elem# | nodei | nodej | thickness | mat#

1	1	2	0.040000	100
2	2	3	0.040000	100
3	3	4	0.040000	100
4	4	5	0.040000	100
5	5	6	0.040000	100
6	6	7	0.040000	100
7	7	8	0.040000	100
8	8	9	0.040000	100
9	9	10	0.040000	100



Equation Constraints are determined by defining the degree of freedom of 1 node in terms of another.

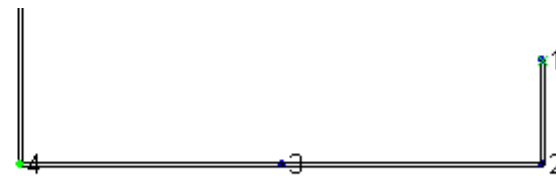
For example, the expression below in Constraints says

At node 1, set degree of freedom 2 equal to 1.0 times node 10, degree of freedom 2:

$$w_1 = 1.0w_{10}$$

You can enter as many constraints as you like, but once you use a degree of freedom on the left hand side of the equation it is eliminated and can not be used again.

Symbols appear on the nodes that you have written constraint equations on, as shown in this plot for nodes 1 and nodes 10.



**Lengths** ?

1.0 2.0 3.0 4.0 5.0 6.0 7.0 8.0 9.0 10.0 11.0 12.0 13.0 14.0 15.0 20.0 30.0 40.0 50.0 60.0 70.0 80.0 90.0 100.0 200.0 300.0 400.0 500.0 600.0 700.0 800.0 900.0 1000.0

**Springs** ?

node# | DOF(x=1,z=2,y=3,theta=4) | kspring | kflag

0

**Constraints** ?

node#e | DOFe | coeff. | node#k | DOFk

1 2 1.000 10 2



### Material Properties

mat# | Ex | Ey | vx | vy | Gxy

100 29500.00 29500.00 0.30 0.30 11346.15

Buttons: C/Z template, Double Elem., help

### Nodes

node# | x | z | xdof | zdof | ydof | qdof | stress

1	5.00	1.00	1	1	1	1.00
2	5.00	0.00	1	1	1	1.00
3	2.50	0.00	1	1	1	1.00
4	0.00	0.00	1	1	1	1.00
5	0.00	3.00	1	1	1	1.00
6	0.00	6.00	1	1	1	1.00
7	0.00	9.00	1	1	1	1.00
8	2.50	9.00	1	1	1	1.00
9	5.00	9.00	1	1	1	1.00
10	5.00	8.00	1	1	1	1.00

Buttons: Update Plot

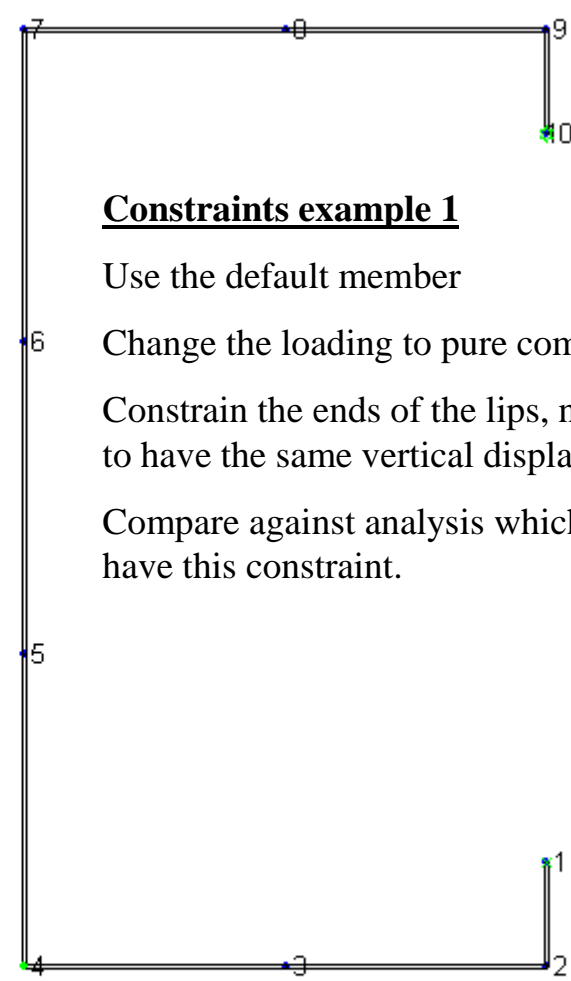
Plot Options:

- node #
- element #
- material #
- stress mag.
- stress dist.
- coordinate:
- constraints
- springs
- origin

### Elements

elem# | nodei | nodej | thickness | mat#

1	1	2	0.040000	100
2	2	3	0.040000	100
3	3	4	0.040000	100
4	4	5	0.040000	100
5	5	6	0.040000	100
6	6	7	0.040000	100
7	7	8	0.040000	100
8	8	9	0.040000	100
9	9	10	0.040000	100



### Constraints example 1

- Use the default member
- Change the loading to pure compression
- Constrain the ends of the lips, nodes 1 and 10 to have the same vertical displacement
- Compare against analysis which does not have this constraint.

### Lengths

1.0 2.0 3.0 4.0 5.0 6.0 7.0 8.0 9.0 10.0 11.0 12.0 13.0 14.0 15.0 20.0 30.0 40.0 50.0 60.0 70.0 80.0 90.0 100.0 200.0 300.0 400.0 500.0 600.0 700.0 800.0 900.0 1000.0

### Springs

node# | DOF(x=1,z=2,y=3,theta=4) | kspring | kflag

0

### Constraints

node#e | DOFe | coeff. | node#k | DOFk

1 2 1.000 10 2

Plot Mode ?

2D  3D  Undef.

half-wavelength

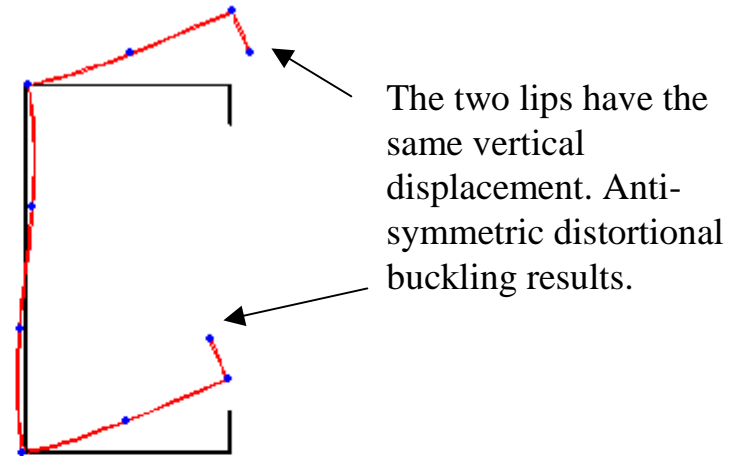
<-- 60 --> ?

Scale 1 S

mode <-- 1 --> ?

file <-- 2 --> ?

Loading is pure compression with a reference stress of 1.0, the two results show the influence of the constraint on the solution.



half-wavelength = 60 load factor = 17.3801 mode = 1

filename = defaultC\_compression\_eq1.mat

filenumber = 2

Plot Curve ?

Min.  Log X

xmin 0

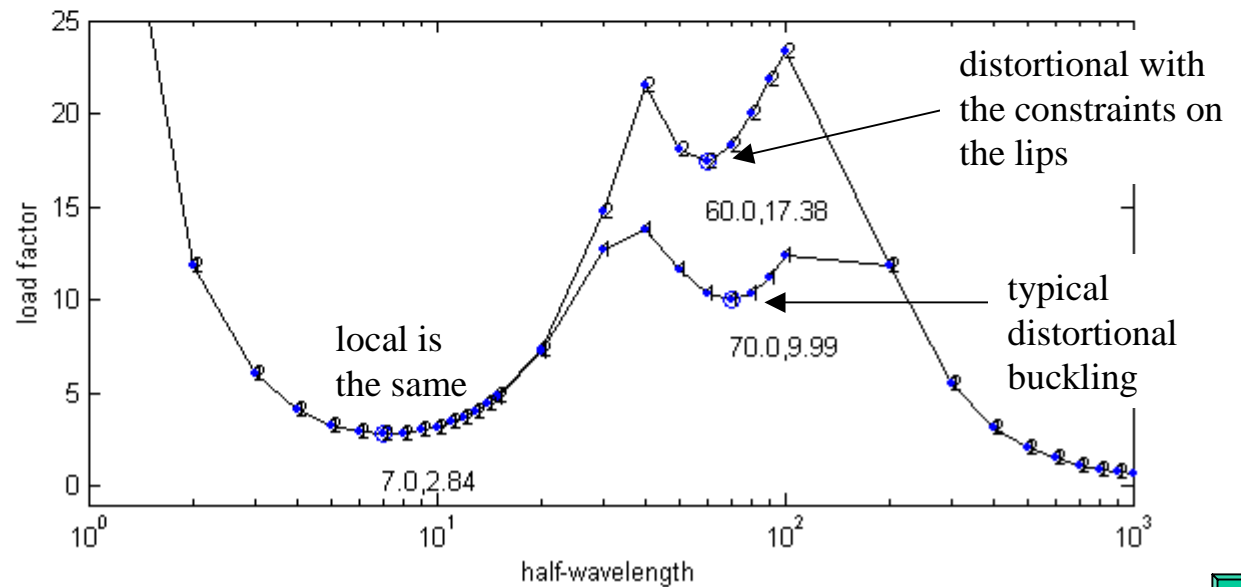
xmax 1000

ymin -1

ymax 25

modes <-- 1 --> ?

plot files = 1 2 ?



**Material Properties** ?  
 mat# | Ex | Ey | vx | vy | Gxy  
 100 29500.00 29500.00 0.30 0.30 11346.15

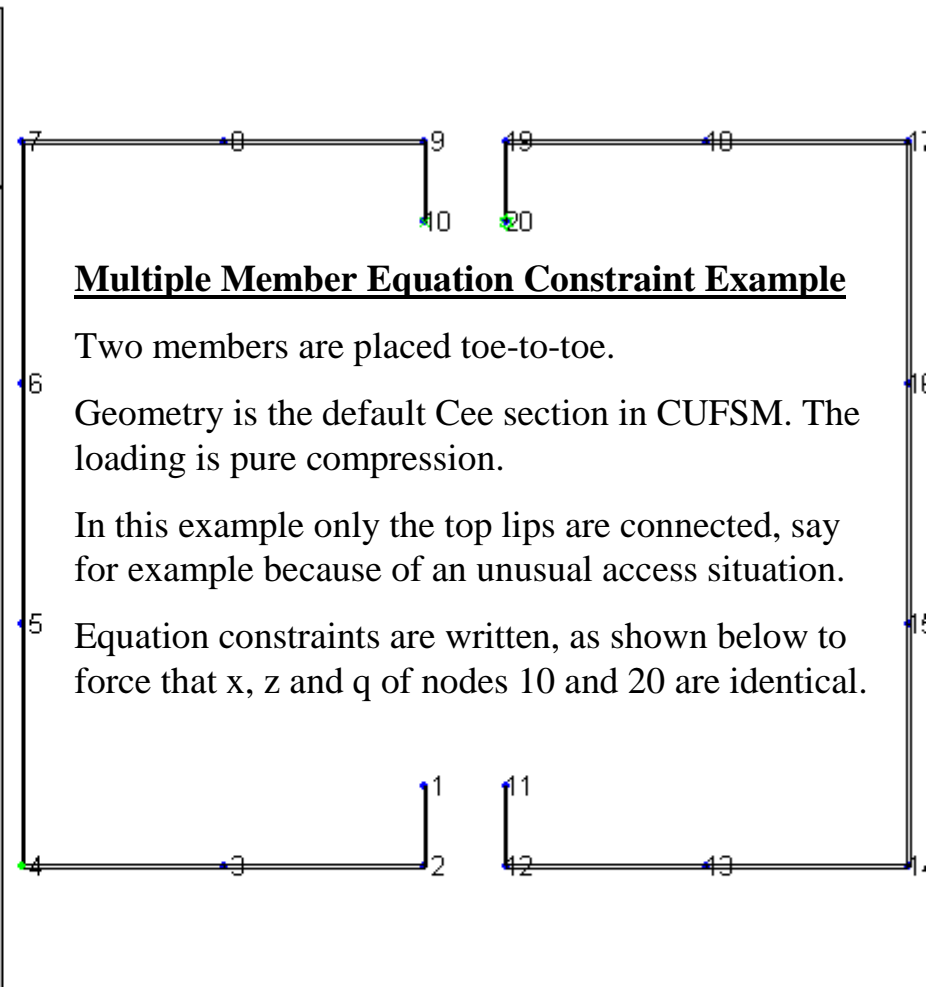
**Nodes** ?  
 node# | x | z | xdof | zdof | ydof | qdof | stress  
 1 5.00 1.00 1 1 1 1.00  
 2 5.00 0.00 1 1 1 1.00  
 3 2.50 0.00 1 1 1 1.00  
 4 0.00 0.00 1 1 1 1.00  
 5 0.00 3.00 1 1 1 1.00  
 6 0.00 6.00 1 1 1 1.00  
 7 0.00 9.00 1 1 1 1.00  
 8 2.50 9.00 1 1 1 1.00  
 9 5.00 9.00 1 1 1 1.00  
 10 5.00 8.00 1 1 1 1.00  
 11 6.00 1.00 1 1 1 1.00

**Elements** ?  
 elem# | nodei | nodej | thickness | mat#  
 1 1 2 0.040000 100  
 2 2 3 0.040000 100  
 3 3 4 0.040000 100  
 4 4 5 0.040000 100  
 5 5 6 0.040000 100  
 6 6 7 0.040000 100  
 7 7 8 0.040000 100  
 8 8 9 0.040000 100  
 9 9 10 0.040000 100  
 10 11 12 0.040000 100

C/Z template  
 Double Elem.  
 help

Update Plot

Plot Options:  
 node #  
 element #  
 material #  
 stress mag.  
 stress dist.  
 coordinate:  
 constraints  
 springs  
 origin



**Lengths** ?  
 1.0 2.0 3.0 4.0 5.0 6.0 7.0 8.0 9.0 10.0 11.0 12.0 13.0 14.0 15.0 20.0 30.0 40.0 50.0 60.0 70.0 80.0 90.0 100.0 200.0 300.0 400.0 500.0 600.0 700.0 800.0 900.0 1000.0

**Springs** ?  
 node# | DOF(x=1,z=2,y=3,theta=4) | kspring | kflag  
 0

**Constraints** ?  
 node#e | DOFe | coeff. | node#k | DOFk  
 10 1 1.000 20 1  
 10 2 1.000 20 2  
 10 4 1.000 20 4

Plot Mode ?

2D  3D  Undef.

half-wavelength

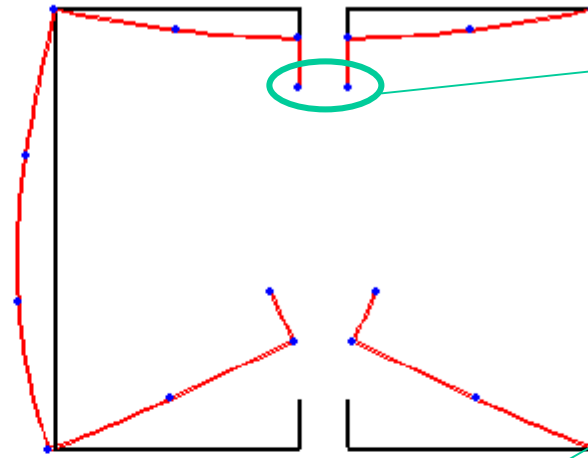
<-- 60 --> ?

Scale 1 S

mode <-- 1 --> ?

file <-- 2 --> ?

Local buckling is not affected by the constraint, but distortional buckling and long wavelength buckling is...



top lips are connected. This has an influence on distortional buckling, as shown.

half-wavelength = 60 load factor = 12.37 mode = 1

filename = two\_defaultCs\_comp.mat

filenumber = 2

Plot Curve ?

Min.  Log X

xmin 0

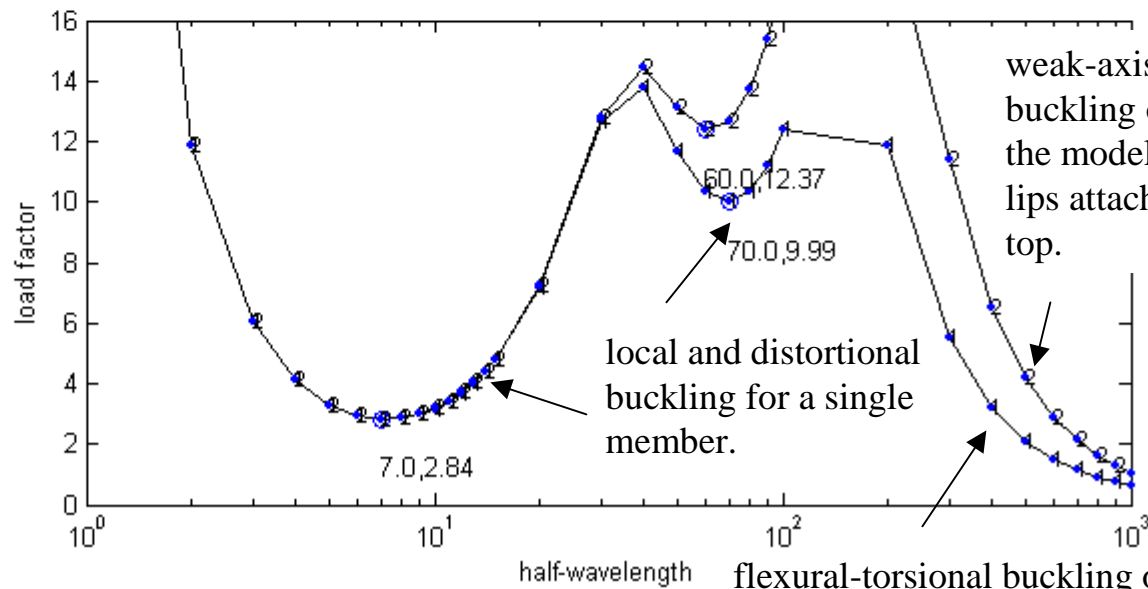
xmax 1000

ymin 0

ymax 16

modes <-- 1 --> ?

plot files = 1 2 ?



weak-axis flexural buckling occurs in the model with the lips attached at the top.

local and distortional buckling for a single member.

flexural-torsional buckling occurs in the single isolated member



# Springs

- External springs may be attached to any node.
- Modeling continuous restraint may use this feature
  - Continuous sheeting attached to a bending member might be considered as springs
  - Sheathing or other materials attached to compression members might be considered as springs
- Springs may be modeled as a constant value, or as varying with the length of the model (i.e. a foundation)

# Springs

- How to
- Sheeting attached to a purlin
- Spring verification problem



### Material Properties

mat# | Ex | Ey | vx | vy | Gxy

100 29500.00 29500.00 0.30 0.30 11346.15

Buttons: C/Z template, Double Elem., help

### Nodes

node# | x | z | xdof | zdof | ydof | qdof | stress

1	2.50	0.63	1	1	1	-44.76
2	2.39	0.49	1	1	1	-45.93
3	2.28	0.36	1	1	1	-47.01
4	2.17	0.23	1	1	1	-48.09
5	2.06	0.09	1	1	1	-49.25
6	2.02	0.05	1	1	1	-49.58
7	1.97	0.02	1	1	1	-49.83
8	1.91	0.01	1	1	1	-49.92
9	1.86	0.00	1	1	1	-50.00
10	1.46	0.00	1	1	1	-50.00
11	1.06	0.00	1	1	1	-50.00

Buttons: Update Plot

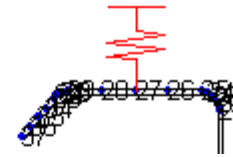
Plot Options:

- node #
- element #
- material #
- stress mag.
- stress dist.
- coordinate:
- constraints
- springs
- origin

### Elements

elem# | nodei | nodej | thickness | mat#

1	1	2	0.070000	100
2	2	3	0.070000	100
3	3	4	0.070000	100
4	4	5	0.070000	100
5	5	6	0.070000	100
6	6	7	0.070000	100
7	7	8	0.070000	100
8	8	9	0.070000	100
9	9	10	0.070000	100
10	10	11	0.070000	100



Springs are determined by defining the node where a spring occurs, what degree of freedom the spring acts in, the stiffness of the spring, and whether or not the spring is a constant value (e.g. force/length) or a foundation spring (e.g. (force/length)/length).

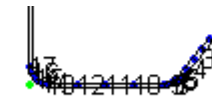
Constant springs use  $k_{flag}=0$ , foundations use  $k_{flag}=1$ .

You can enter as many springs as you like.

The springs always go to “ground”. Therefore they cannot be used to connect two members.

Springs appear in the picture of your model once you define them.

Springs are modeled as providing a continuous contribution along the length.



### Lengths

1.1 1.4 1.7 2.0 2.4 2.9 3.5 4.2 5.1 6.2 7.4 9.0 10.8 13.1 15.8 19.0 23.0 27.7 33.4 40.3 48.7 58.8 70.9 85.6 103.3 124.6 150.4 181.5 219.0 264.3 319.0 384.9 464.5 560.6 676.5 8

### Springs

node# | DOF(x=1,z=2,y=3,theta=4) | kspring | kflag

27 2 1.000 1

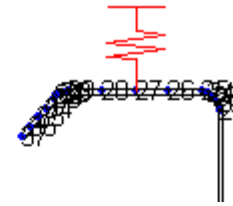
### Constraints

node#e | DOFe | coeff. | node#k | DOFk

0



<b>Material Properties</b> <span>?</span> mat#   Ex   Ey   vx   vy   Gxy 100 29500.00 29500.00 0.30 0.30 11346.15		C/Z template Double Elem. help
<b>Nodes</b> <span>?</span> node#   x   z   xdof   zdof   ydof   qdof   stress		Update Plot Plot Options: <input checked="" type="checkbox"/> node # <input type="checkbox"/> element # <input type="checkbox"/> material # <input type="checkbox"/> stress mag. <input type="checkbox"/> stress dist. <input type="checkbox"/> coordinate: <input checked="" type="checkbox"/> constraints <input checked="" type="checkbox"/> springs <input checked="" type="checkbox"/> origin
<b>Elements</b> <span>?</span> elem#   nodei   nodej   thickness   mat#		



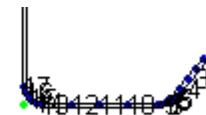
### Purlin with a sheeting “spring” example

Use the LGSI Z 12 x 2.5 14g model from Tutorial 3

The applied bending stress is restrained bending about the geometric axis with  $f_y=50$  ksi. (first yield is in tension in this model as the flange widths are slightly different sizes)

Assume a spring of  $k = 1.0$  (kip/in.)/in. exists in the vertical direction at mid-width of the compression flange. (Ignore, in this case, rotational stiffness contributions from the sheeting, etc.)

See Springs below for the definition of the vertical spring.



<b>Lengths</b> <span>?</span> 1.1 1.4 1.7 2.0 2.4 2.9 3.5 4.2 5.1 6.2 7.4 9.0 10.8 13.1 15.8 19.0 23.0 27.7 33.4 40.3 48.7 58.8 70.9 85.6 103.3 124.6 150.4 181.5 219.0 264.3 319.0 384.9 464.5 560.6 676.5 8'	
---	--

<b>Springs</b> <span>?</span> node#   DOF(x=1,z=2,y=3,theta=4)   kspring   kflag 27 2 1.000 1
---

<b>Constraints</b> <span>?</span> node#e   DOFe   coeff.   node#k   DOFk 0
--

Plot Mode ?

2D  3D  Undef.

half-wavelength

<-- 23 --> ?

Scale 1 S

mode <-- 1 --> ?

file <-- 2 --> ?

loaded files:  
 1 = LGSI-Z-12-25-14g.mat  
 2 = LGSI-Z-12-25-14g-kz1.mat  
 3 = LGSI-Z-12-25-14g-kz1\_2.mat

Plot Curve ?

Min.  Log X

xmin 0

xmax 400

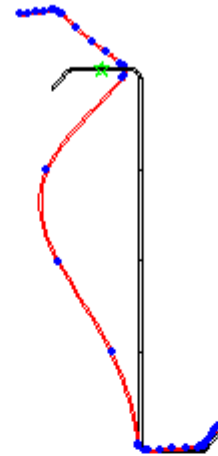
ymin 0

ymax 2.5

modes <-- 1 --> ?

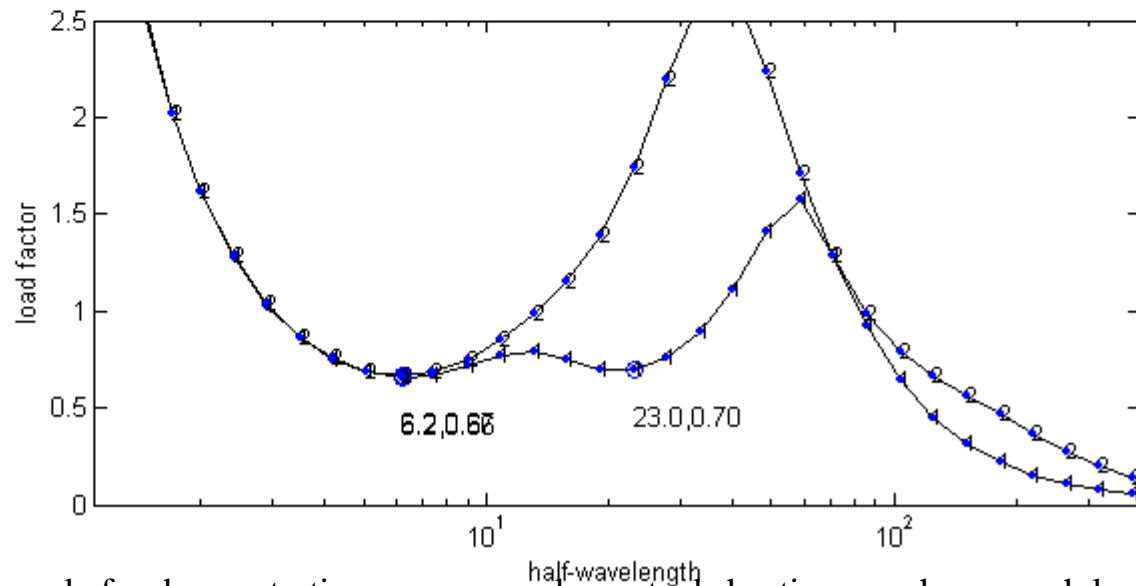
plot files = 1 2 ?

The buckling curve below shows the results of an analysis without the springs (1) and analysis with the spring (2). Note that the spring has greatly increased the distortional buckling stress.



The buckling mode to the left shows distortional buckling with the spring in place. Note, the “star” denotes the existence of the spring in the model.

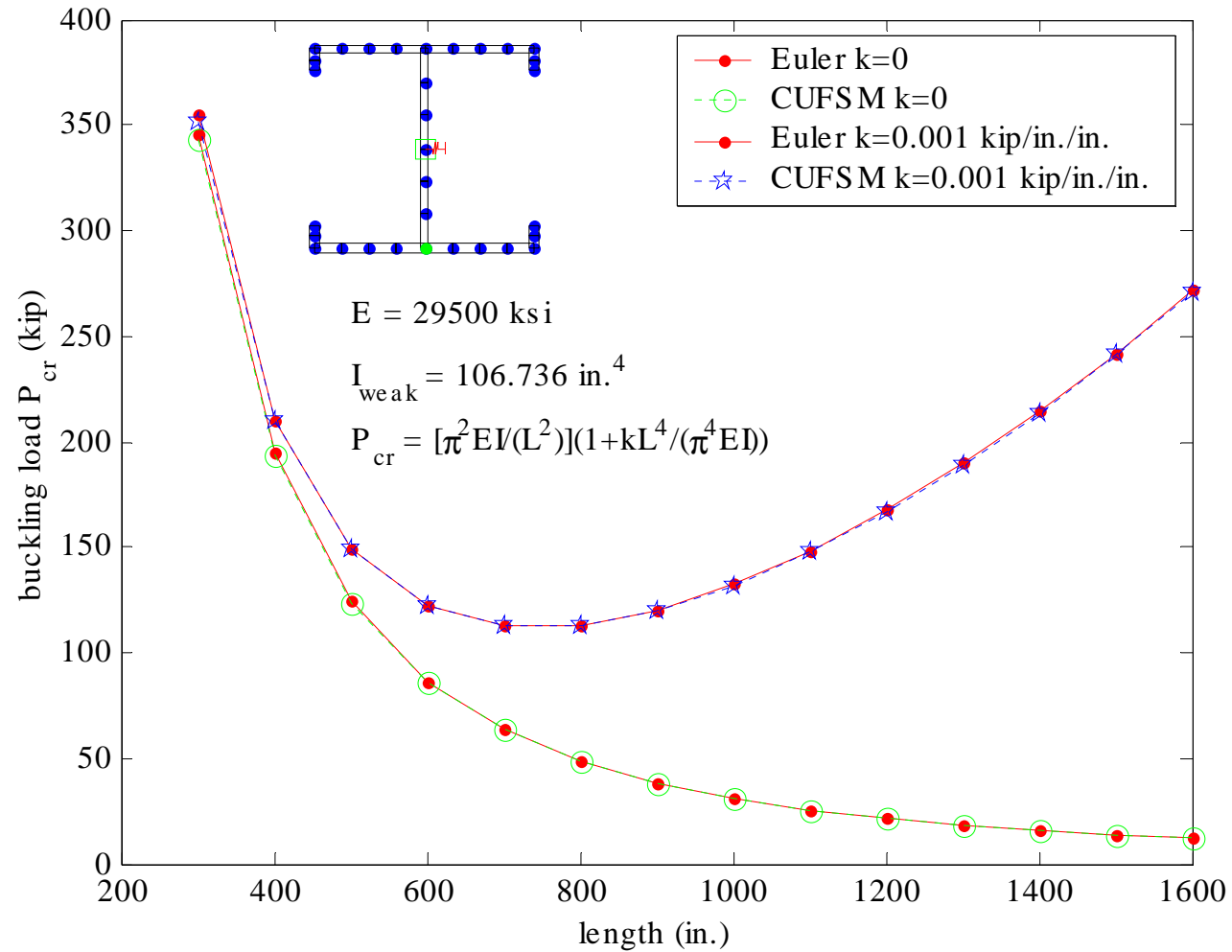
half-wavelength = 23 load factor = 1.7408 mode = 1  
 filename = LGSI-Z-12-25-14g-kz1.mat  
 filenumber = 2



Example for demonstrative purposes only - actual sheeting may have much lower stiffness, and other factors may be considered in the analysis.



# Spring verification



# Multiple materials

- Multiple materials may be used in a single CUFSM model
- Explicitly modeling attachments that are of different materials may use this feature
- Some unusual geometry changes may be modeled by changing the material properties



### Material Properties

mat# | Ex | Ey | vx | vy | Gxy

100	29500.00	29500.00	0.30	0.30	11346.15
200	2950.00	2950.00	0.30	0.30	1134.62

C/Z template  
Double Elem.  
help

### Nodes

node# | x | z | xdof | zdof | ydof | qdof | stress

1	5.00	1.00	1	1	1	1.00
2	5.00	0.00	1	1	1	1.00
3	2.50	0.00	1	1	1	1.00
4	0.00	0.00	1	1	1	1.00
5	0.00	3.00	1	1	1	1.00
6	0.00	6.00	1	1	1	1.00
7	0.00	9.00	1	1	1	1.00
8	2.50	9.00	1	1	1	1.00
9	5.00	9.00	1	1	1	1.00
10	5.00	8.00	1	1	1	1.00
11	6.00	1.00	1	1	1	1.00

Update Plot

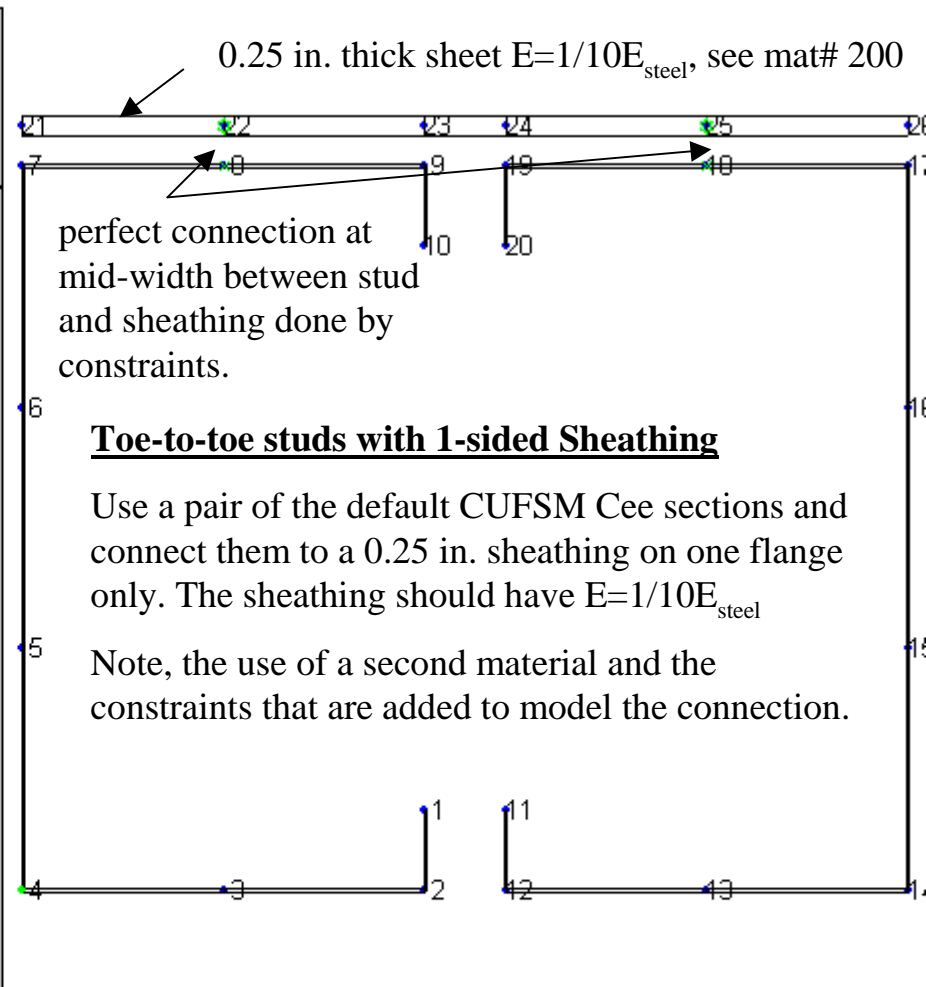
Plot Options:

- node #
- element #
- material #
- stress mag.
- stress dist.
- coordinate:
- constraints
- springs
- origin

### Elements

elem# | nodei | nodej | thickness | mat#

1	1	2	0.040000	100
2	2	3	0.040000	100
3	3	4	0.040000	100
4	4	5	0.040000	100
5	5	6	0.040000	100
6	6	7	0.040000	100
7	7	8	0.040000	100
8	8	9	0.040000	100
9	9	10	0.040000	100
10	11	12	0.040000	100



### Lengths

1.0 2.0 3.0 4.0 5.0 6.0 7.0 8.0 9.0 10.0 11.0 12.0 13.0 14.0 15.0 20.0 30.0 40.0 50.0 60.0 70.0 80.0 90.0 100.0 200.0 300.0 400.0 500.0 600.0 700.0 800.0 900.0 1000.0

### Springs

node# | DOF(x=1,z=2,y=3,theta=4) | kspring | kflag

0
---

### Constraints

node#e | DOFe | coeff. | node#k | DOFk

8	1	1.000	22	1
18	1	1.000	25	1
8	2	1.000	22	2

### Material Properties

mat# | Ex | Ey | vx | vy | Gxy

100	29500.00	29500.00	0.30	0.30	11346.15
200	2950.00	2950.00	0.30	0.30	1134.62

C/Z template  
Double Elem.  
help

---

### Nodes

node# | x | z | xdof | zdof | ydof | qdof | stress

1	5.00	1.00	1	1	1	1.00
2	5.00	0.00	1	1	1	1.00
3	2.50	0.00	1	1	1	1.00
4	0.00	0.00	1	1	1	1.00
5	0.00	3.00	1	1	1	1.00
6	0.00	6.00	1	1	1	1.00
7	0.00	9.00	1	1	1	1.00
8	2.50	9.00	1	1	1	1.00
9	5.00	9.00	1	1	1	1.00
10	5.00	8.00	1	1	1	1.00
11	6.00	1.00	1	1	1	1.00

Update Plot

Plot Options:

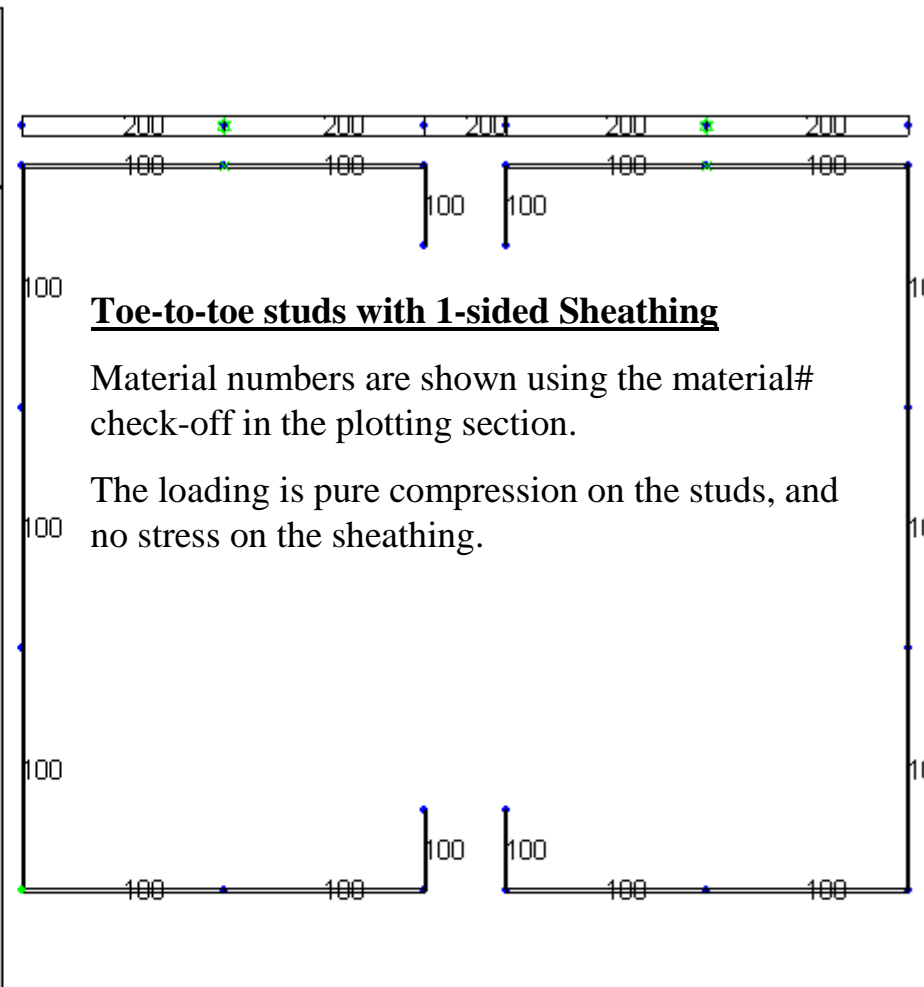
- node #
- element #
- material #
- stress mag.
- stress dist.
- coordinate:
- constraints
- springs
- origin

---

### Elements

elem# | nodei | nodej | thickness | mat#

1	1	2	0.040000	100
2	2	3	0.040000	100
3	3	4	0.040000	100
4	4	5	0.040000	100
5	5	6	0.040000	100
6	6	7	0.040000	100
7	7	8	0.040000	100
8	8	9	0.040000	100
9	9	10	0.040000	100
10	11	12	0.040000	100



### Lengths

1.0 2.0 3.0 4.0 5.0 6.0 7.0 8.0 9.0 10.0 11.0 12.0 13.0 14.0 15.0 20.0 30.0 40.0 50.0 60.0 70.0 80.0 90.0 100.0 200.0 300.0 400.0 500.0 600.0 700.0 800.0 900.0 1000.0

### Springs

node# | DOF(x=1,z=2,y=3,theta=4) | kspring | kflag

0
---

### Constraints

node#e | DOFe | coeff. | node#k | DOFk

8	1	1.000	22	1
18	1	1.000	25	1
8	2	1.000	22	2

Plot Mode ?

2D  3D  Undef.

half-wavelength

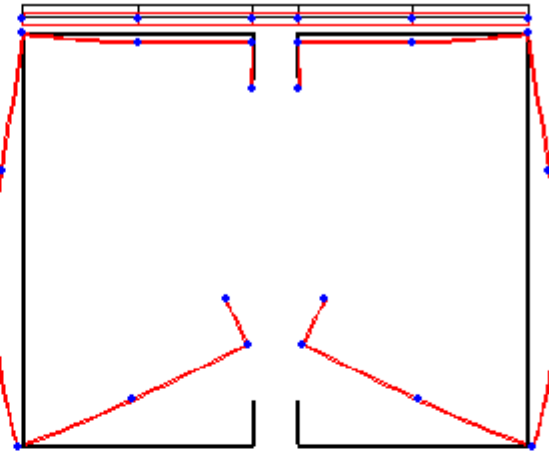
<-- 60 --> ?

Scale 1 S

mode <-- 1 --> ?

file <-- 2 --> ?

Local buckling is not affected by the sheathing, but distortional buckling and long wavelength buckling is...



half-wavelength = 60 load factor = 13.0659 mode = 1

file number = 2 filename = two\_defaultCs\_comp\_sheet.mat

Plot Curve ?

Min.  Log X

xmin 0

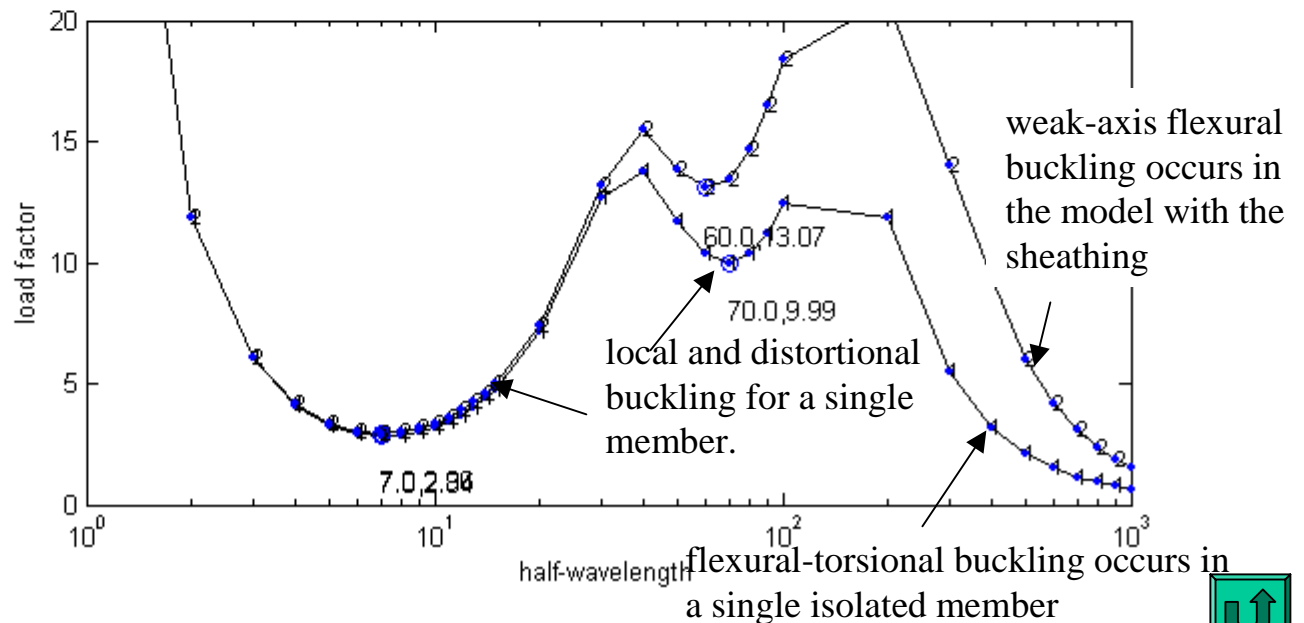
xmax 1000

ymin 0

ymax 20

modes <-- 1 --> ?

plot files = 1 2 ?



# Orthotropic Material

- Orthotropic materials may be used in CUFSM
- Plastics, composites, or highly worked metals may benefit from using this feature



**Material Properties** ?

mat# | E<sub>x</sub> | E<sub>y</sub> | ν<sub>x</sub> | ν<sub>y</sub> | G<sub>xy</sub>

100 29500.00 29500.00 0.30 0.30 5673.00

**Nodes** ?

node# | x | z | xdof | zdof | ydof | qdof | stress

1 0.00 0.00 0 0 1 1 1.00  
 2 2.50 0.00 1 1 1 1 1.00  
 3 5.00 0.00 1 1 1 1 1.00  
 4 7.50 0.00 1 1 1 1 1.00  
 5 10.00 0.00 1 0 1 1 1.00

**Elements** ?

elem# | nodei | nodej | thickness | mat#

1 1 2 0.100000 100  
 2 2 3 0.100000 100  
 3 3 4 0.100000 100  
 4 4 5 0.100000 100

C/Z template

Double Elem.

help

Update Plot

Plot Options:

node #

element #

material #

stress mag.

stress dist.

coordinate:

constraints

springs

origin

### Orthotropic Material Example

Simply supported plate where  $G_{xy}$  is  $1/2G_{\text{isotropic}}$

Low G modulus are typical concerns with some modern plastics and other materials. Also, some sheathing materials may be modeled orthotropically.



**Lengths** ?

4.0 6.0 8.0 10.0 12.0 14.0 16.0 18.0 20.0

**Springs** ?

node# | DOF(x=1,z=2,y=3,theta=4) | kspring | kflag

0

**Constraints** ?

node#e | DOFe | coeff. | node#k | DOFk

0

half-wavelength = 10 load factor = 8.8 mode = 1

Plot Mode ?

2D  3D  Undef.

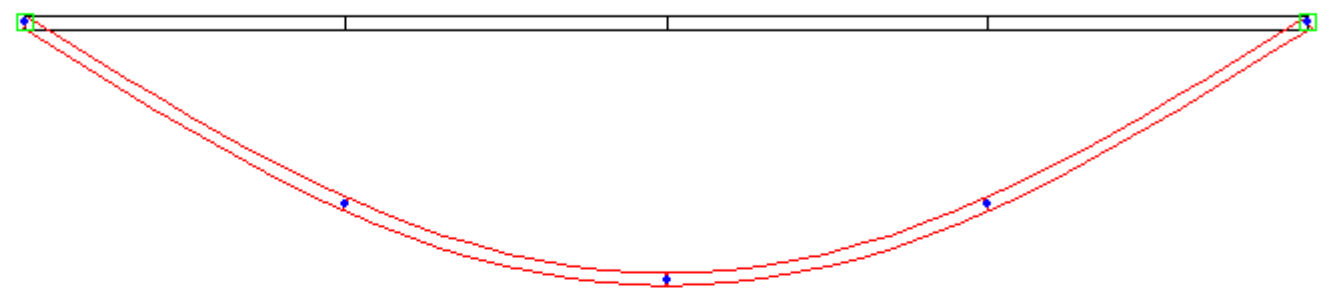
half-wavelength

<-- 10 --> ?

Scale 1

mode <-- 1 --> ?

Stress Distribution ?



Isotropic Theory  $\rightarrow f_{cr} = k \frac{\pi^2 E}{12(1-\nu^2)} \left(\frac{t}{b}\right)^2 = 4 \frac{\pi^2 29500}{12(1-0.3^2)} \left(\frac{0.1}{10.0}\right)^2 = 10.66 \text{ksi}$

vs. 8.80 ksi when  $G_{xy} = 1/2 G_{isotropic}$

Plot Curve ?

Min.  Log X

xmin 0

xmax 20

ymin 0

ymax 20.5569

modes <-- 1 --> ?

Text Output ?

