

# **An Oligopolistic Electricity Market Model with Tradable NO<sub>x</sub> Permits**

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# Outline

## I. Overview of Questions

## II. Model Structure and Computation Approach

## III. Application

*Interaction of PJM Electricity and USEPA NO<sub>x</sub> Budget Program*

*a. Background*

*b. Assumptions*

## IV. Results

*Comparison of perfect competition with different scenarios*

*a. Price*

*b. Social Welfare*

*c. Productive and NO<sub>x</sub> Trading Efficiency*

*d. Strategy Rationale*

## V. Conclusion

THIS SLIDE SHOULD BE OMITTED IN A  
10 MINUTE TALK, WILL TAKE TOO  
LONG (YOU SHOULD PRACTICE YOUR  
TALK TO SEE WHICH SLIDES CAN BE



*What might be the effect of policies concerning...*

- Generation structure (mergers, ownership, distributed resources, entry...)
- Transmission investment (new lines...)
- Market rules
  - Transmission pricing (taxes, congestion pricing, counterflows, zonal ...)
  - Access (retail load, generators, arbitragers ...)
  - Environmental markets (green certs., CO2 trading ...)

DONE QUICKLY AND WHICH SEEM LIKE  
DISTRACTIONS

*...upon...*

- Economic efficiency (allocative & productive efficiency)
- Income distribution (TSO revenues, profits, consumer surplus)
- Emissions

*...considering generator strategic behavior?*

- Bidding
- Capacity withdrawal
- Manipulation of transmission (deliberate congestion, decongestion)
- Manipulation of emissions markets (withholding of allowances)\*\*\*\*\*

## II. Model Structure and Computational Approach: Direct Solution of Equilibrium Conditions

### Producer A

Choose gen &  
sales to  
maximize profit  
s.t. capacity  
 $\Rightarrow$  1<sup>st</sup> order  
conditions



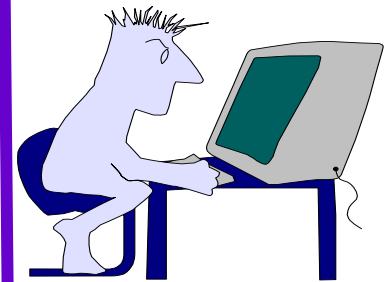
### Producer B

Choose gen &  
sales to  
maximize profit  
s.t. capacity  
 $\Rightarrow$  1<sup>st</sup> order  
conditions

ISO: Choose Transmission Flows to Max Value of Network  
s.t. transmission constraints  $\Rightarrow$  1<sup>st</sup> order conditions

Consumers: Max Value - Expenditures (Demand Curve)

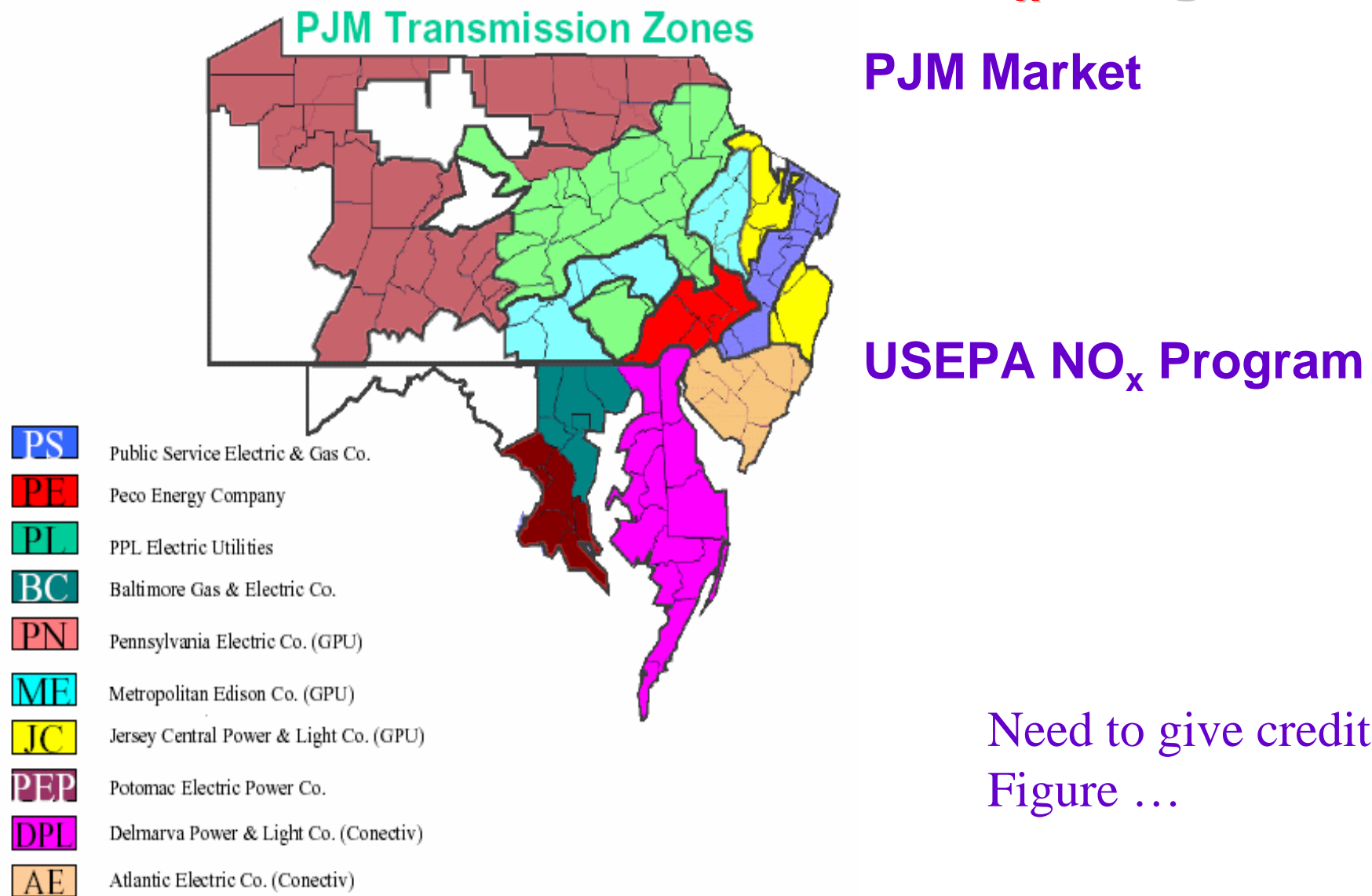
Market Clearing Conditions



1. Derive first-order conditions for each player
2. Impose market clearing conditions
3. Solve resulting system of conditions (*complementarity problem*)

# III. Application Background

## PJM Market and USEPA NO<sub>x</sub> Program

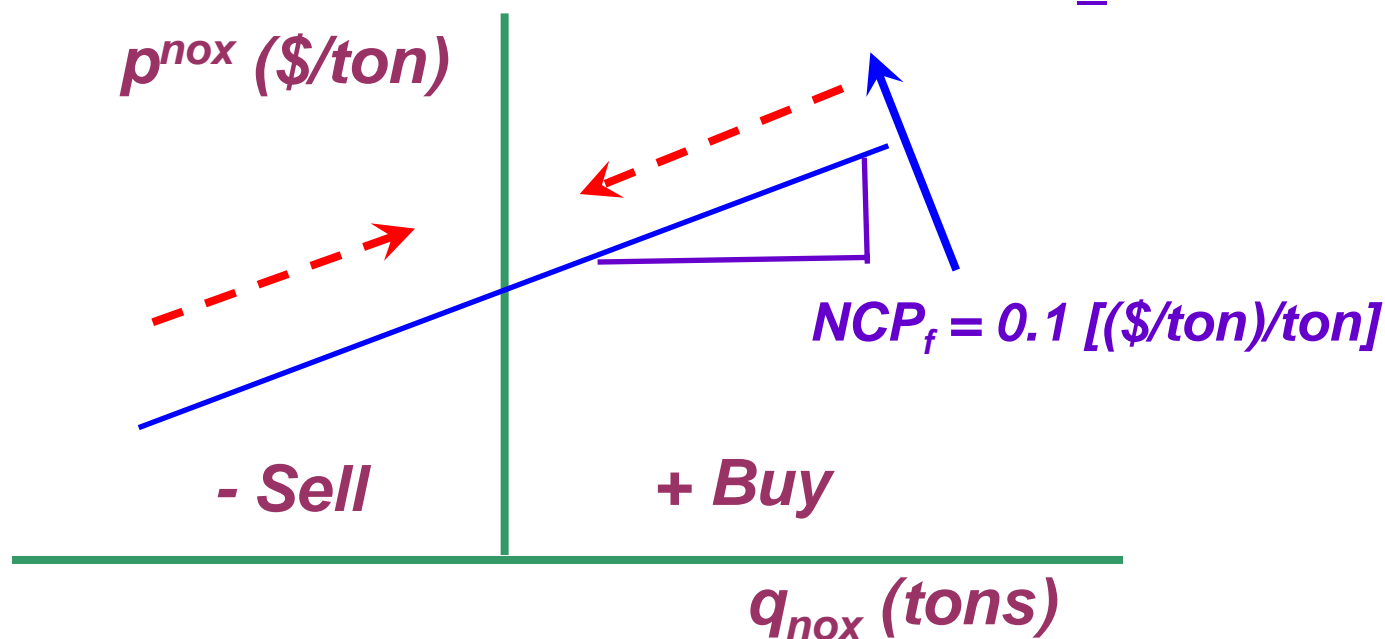


# Model Assumptions

- **Network and Load**
  - *Load duration curve (LCD) approximated by 5 blocks*
  - *Only 500 kV line → 14 nodes, 18 arcs*
  - *No transmission losses*
  - *Power Transfer and Distribution Factors (PTDFs)*
- **Producers**
  - *791 generators*
  - *6 largest producers (capacity share: 4% to 18%)*
    - *Cournot strategy in electricity market*
    - *Conjectured pricing in  $\text{NO}_x$  market*
  - *Remaining produces price takers (3 producers)*
- **Consumer**
  - *Linear demand Curve*
- **ISO**
- **Importer**

# NO<sub>x</sub> Conjectured Pricing

Producer's belief regarding its action on NO<sub>x</sub> price



$qNO_x$ : Net Position in NO<sub>x</sub> permit market → Sell (-) and Buy (+)

# Scenarios Investigated

## A. Perfect competition (COMP)

- Price-taking behavior in power & allowances markets

## B. Oligopoly in electricity market (CONOURT)

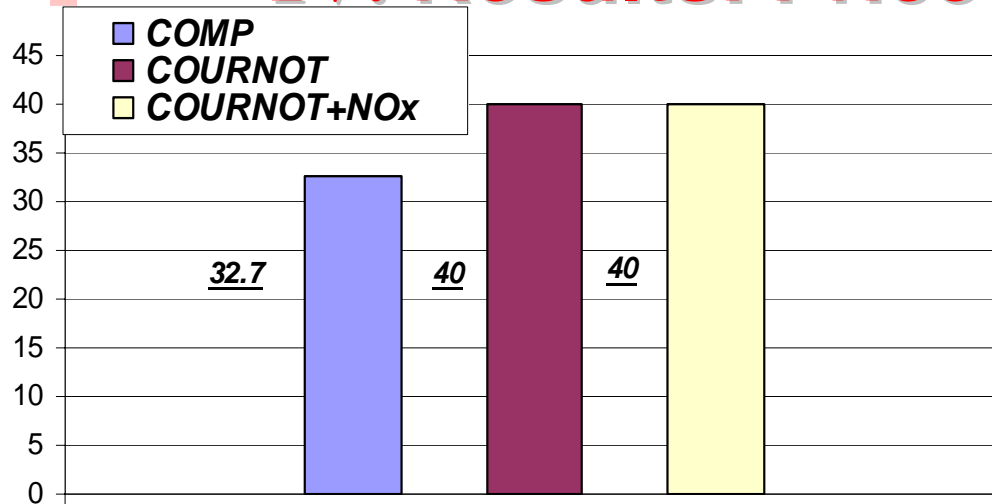
*Cournot strategy for 6 largest in electricity market*

- No Conjectured NO<sub>x</sub> Pricing

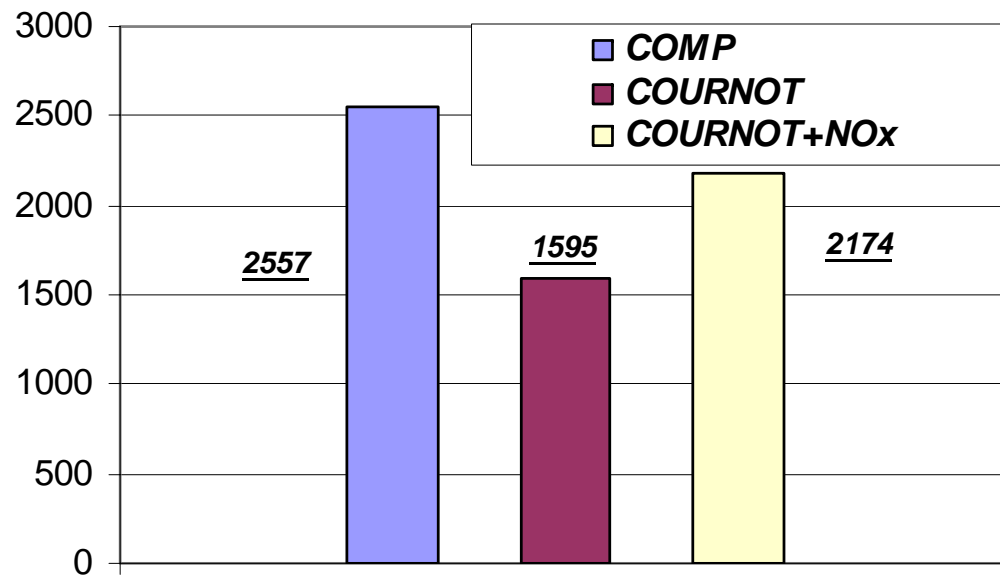
## C. Oligopoly in both markets (CONOURT+NO<sub>x</sub>)

- For 6 largest producers: Cournot strategy in electricity market plus Conjectured NO<sub>x</sub> Pricing in NO<sub>x</sub> market
  - $NCP_{2,3,5,6,7} = 0.1$  [(\$/ton)/ton]
  - $NCP_4 = 1.5$  [(\$/ton)/ton] ← The largest producer with a long position in the NO<sub>x</sub> market

## IV. Results: Price Comparison



Sale-Weighted Electricity Price(\$/MWh)



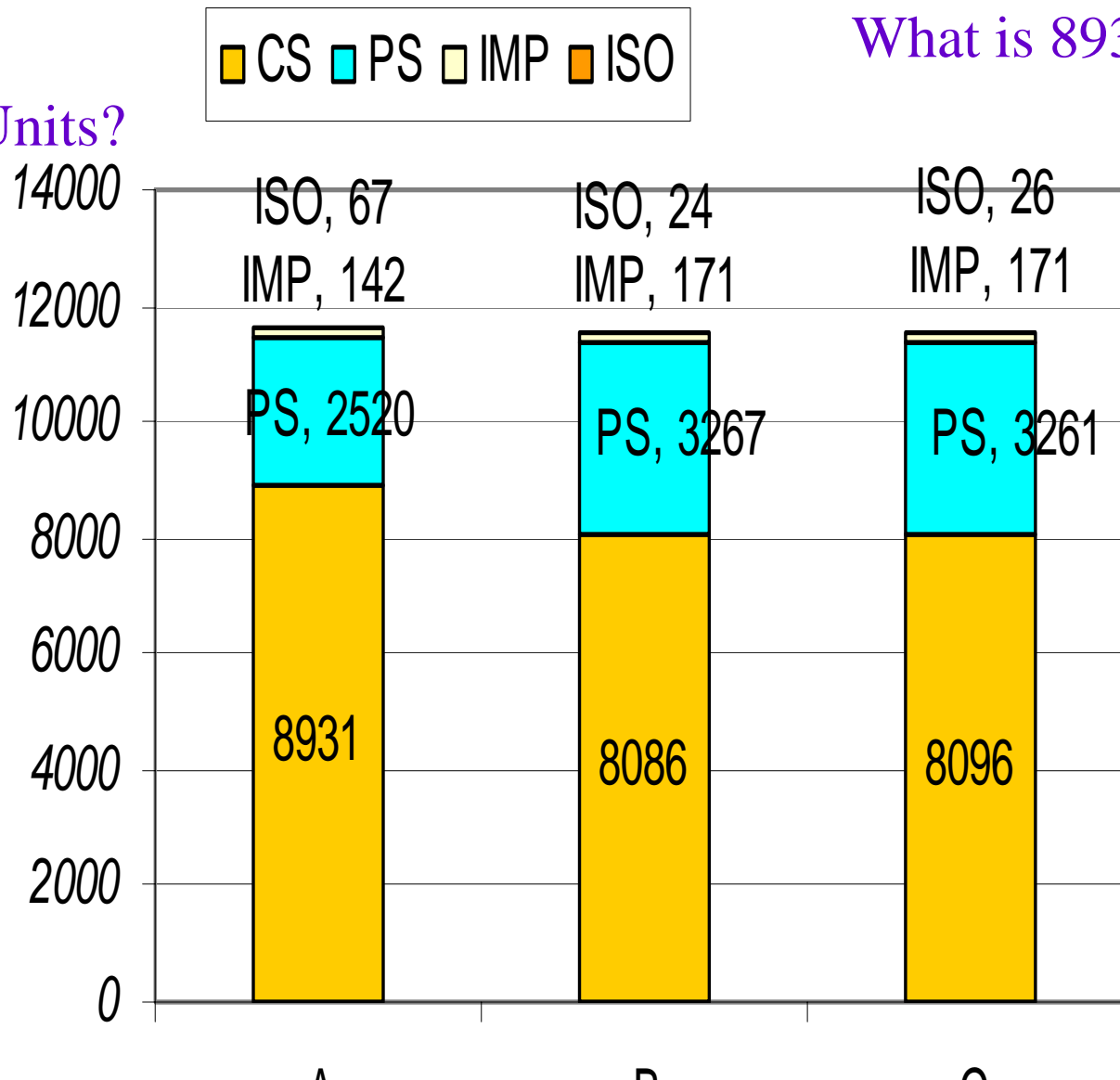
NOx Permit Price (\$/ton)

- *Price of electricity goes up as producers restrain output*
- *Peak period electricity price increase by 37% and 34% compared with COMP for COURNOT and COURNOT+NO<sub>x</sub>, respectively*
- *Price of NO<sub>x</sub> decreases as a result of producers reducing energy output, suppressing NO<sub>x</sub> permit demand*
- *Producer 4 drives up NO<sub>x</sub> permit price if strategic in emissions market (HOW??)*

# Welfare Analysis: Compared to Competitive Scenario

Can't see total welfare (should show)  
What is 8931? (Label as CS)

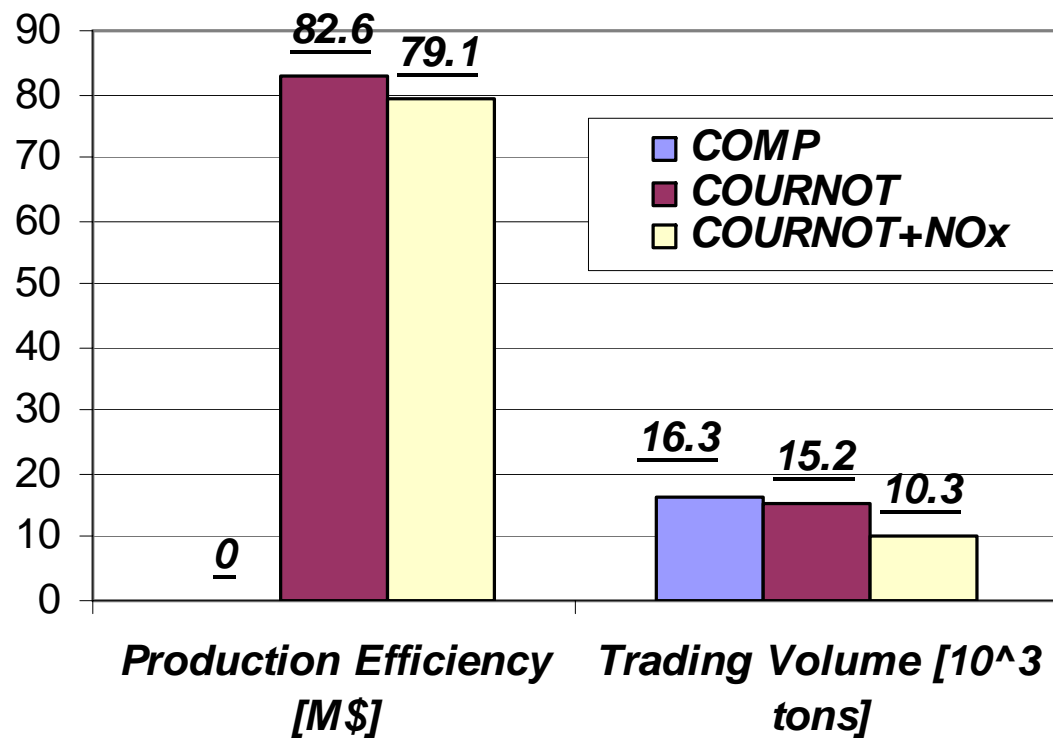
Units?



- **SW (social welfare) declines by 112 and 106 [M\$/yr] for Cournot solutions**
- **PS (producer surplus) goes up as producers exercise market power**
- **IMP (Importer) revenue goes up as electricity prices go up**
- **ISO revenue goes down as less power being transferred**

# Efficiency Comparison

## Compared to Competitive Scenario



### Definition of measurement:

#### a. Productive Inefficiency

$$= (GC_i - GC_{COMP} / \text{load}^*) [M\$]$$

#### b. NO<sub>x</sub> Trading Inefficiency

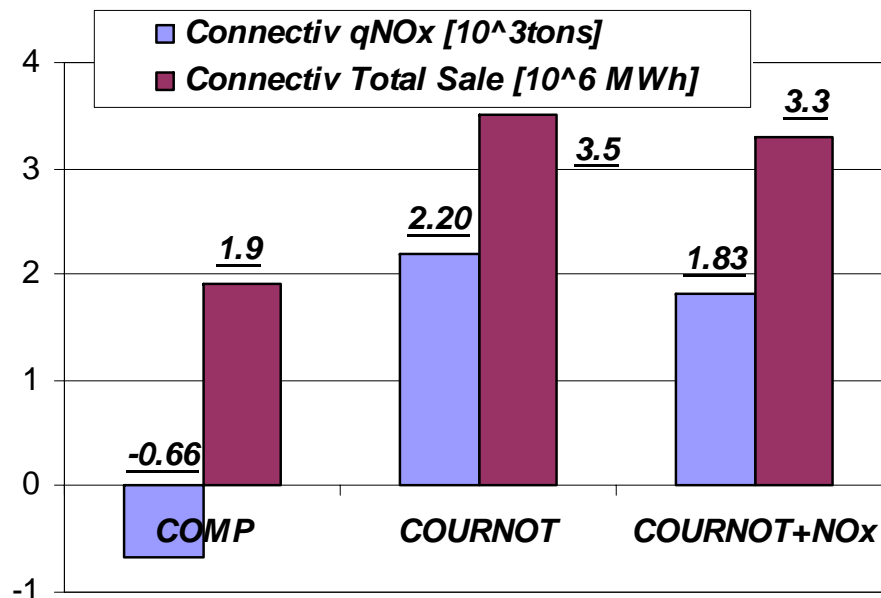
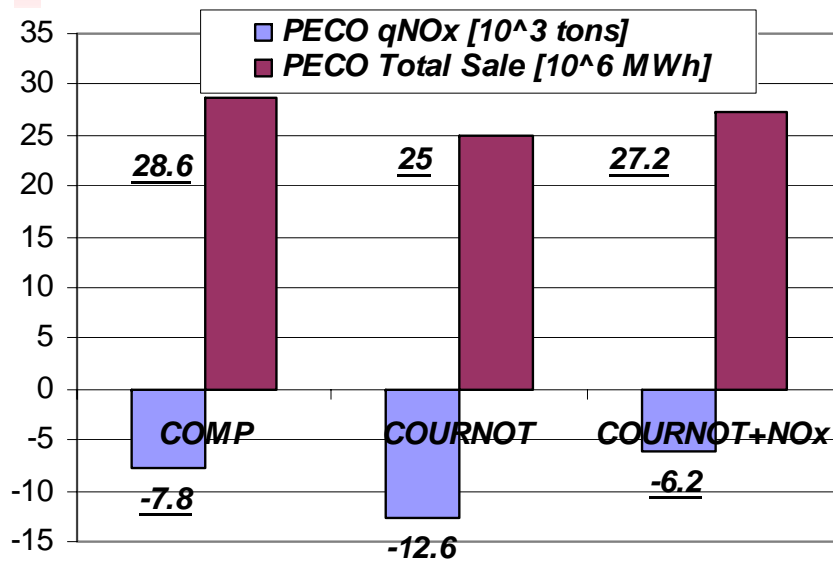
$$= (\text{Trade}^{\text{NO}_x}_i - \text{Trade}^{\text{NO}_x}_{COMP}) [10^3 \text{ tons}]$$

### Market power leads to:

a. A 8.0% and 7.7% of productive inefficiency for COUNOT and COUNOT+NO<sub>x</sub>

b. A 6.8% and 36.5% decrease in NO<sub>x</sub> trading volume

# Player Strategies in NO<sub>x</sub> Market



(Net Sale of Permits - qNO<sub>x</sub> [tons]:  
Sell (-)/Buy(+))

## • PECO: Compare with COMP

- Restrain output and sell more NO<sub>x</sub> permits in COUNOT → price falls from \$2,557 to \$1,595
- Expand output and sell fewer NO<sub>x</sub> permit in COUNOT+NO<sub>x</sub> → Price falls only to \$2,174

## • Connectiv: Compare with COMP

- Increase output by 84% due to higher electricity prices in COUNOT → become net buyer in NO<sub>x</sub> market
- Shrink output by 6% in COUNOT+NO<sub>x</sub> compared with COUNOT due to higher costs associated with NO<sub>x</sub> permits

## V. Conclusion

- *Interactions between electricity and NO<sub>x</sub> market can be investigated by Cournot and conjectured NO<sub>x</sub> pricing assumptions in a large-scale model*
- *Detailed representation of market allows a variety of welfare and efficiency analyses, and to gain insight on players' strategy*
- *The model is capable of answering various policy questions, such as:*
  - *“What would the NO<sub>x</sub> price be if the CAP is imposed over entire year?” This is not an exciting conclusion to end with. Have more questions pointing to future research (e.g., optimal manipulation of NO<sub>x</sub> market)*